

**SIMILITUDE CONSIDERATIONS IN NEUTRON  
AND GAMMA RAY SCATTERING**

---

**Kenneth C. Ney**

Library  
U. S. Naval Postgraduate School  
Monterey, California









8P





SIMULATED COLLISION ACTIONS IN NEUTRON  
AND GAMMA RAY SCATTERING

by

Kenneth C. Noy

A Thesis Submitted to the  
Graduate Faculty in Partial Fulfillment of  
The Requirements for the Degree of  
MASTER OF SCIENCE

Major Subject: Nuclear Engineering



U. S. GOVERNMENT

	Page
I. INTRODUCTION	1
II. SCOPE OF THE STUDY	2
III. SCOPE OF THE STUDY	4
IV. SCOPE OF THE STUDY	5
A. Assumptions	5
B. Neutron Scattering	10
C. Gamma Ray Scattering	27
V. SCOPE OF THE STUDY	32
A. Materials	32
B. Equipment	33
C. Procedure	37
VI. SCOPE OF THE STUDY	43
A. Neutron Scattering	43
B. Gamma Ray Scattering	47
C. General Information	50
VII. SCOPE OF THE STUDY	52
VIII. SCOPE OF THE STUDY	53
IX. SCOPE OF THE STUDY	54
A. SCOPE OF THE STUDY	55
A. Sample Neutron Scattering	55

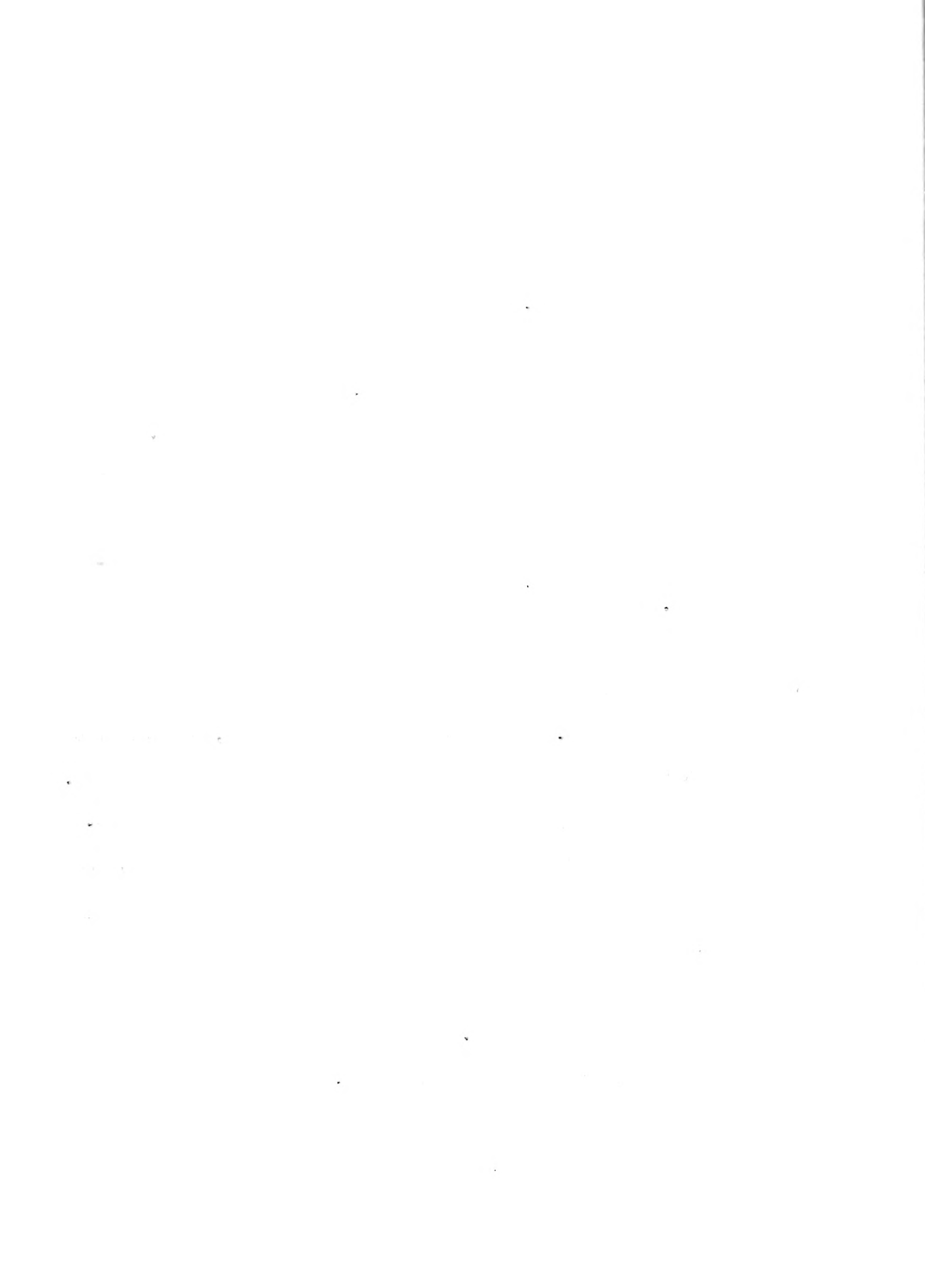


## I. INTRODUCTION

The current development of nuclear powered aircraft involves many problems which are relatively unimportant in the design of large permanently located reactors. One of these problems is the design of shielding arrangements which will materially reduce the weight of the shield and yet sufficiently protect the crew. One possibility is the use of a shadow shield between the reactor and the crew compartment. Another is a split shield where the shielding placed next to the reactor reduces the radiation to some degree and additional shielding placed around the crew compartment reduces the radiation within the compartment to permissible levels.

With a shielding arrangement of these or similar types some of the reactor-produced neutron and gamma-ray radiation will be scattered by the structure of the aircraft. To design the shield properly, the amount of this scattered radiation that enters the crew compartment must be found. This can either be done by mathematical or direct measurement methods. Considering the complex structure that an airplane necessarily has, the latter method employing a model of the airplane is probably the more feasible way.

Thus, the relationship between the scattering by the model and the full-scale structure must be known. This relationship with a simplified structure was the object of this investigation.



## II. REVIEW OF LITERATURE

No investigations on the subject of similitude considerations in the scattering of neutrons and gamma rays by structural material were found in the literature. However, many studies related to this subject are available.

Glasgow (1) investigated the scattering of neutrons from the walls and air of a laboratory by suspending from the center of the ceiling a source and detector at various distances above the floor of a cubic room. The expressions he used for calculating the expected scattering were for an infinite air medium and for the flux of scattered neutrons returning to a source when the source is midway between two non-capturing semi-infinite media, here the walls.

Plesset (2) developed formulas for the intensity of gamma rays scattered by air from a source to a receiver but restricted his analysis to single scattering. He made similar calculations for the intensity of neutrons singly scattered by air from a source to a receiver. He also developed approximate expressions for the reflection of gamma rays and neutrons from a semi-infinite slab.

As a continuation of this, Plesset and others (3) illustrated by exact calculations the geometrical effects of the size of a shadow shield and a source on the intensity of gamma rays scattered into a receiver.

The gamma ray backscattering from various materials was investigated experimentally and qualitatively by Hine and McCall (4). The experimental procedure involved placing a point source on or having it suspended over





the horizontally placed scattering material with a NaI(Tl) crystal detector placed vertically above the source. The results were plotted to show the relationship between the scattered gamma rays and the energy of the primary gamma radiation for the various geometries used.

Plesset and Cohen (5) presented formulas for the calculation of the differential cross section  $d\sigma/d\Omega$  for the scattering of gamma rays into an element of solid angle and gave a graph of  $d\sigma/d\Omega$  versus the angle of scatter. Also, the development of an expression for the intensity of the gamma radiation at a point in an infinite medium due to the direct radiation and scattered radiation was given.

All of these investigations were made with point receivers and with what can be considered infinite or semi-infinite scattering media. In the problem investigated in this thesis detectors of finite size were used as the receivers and thin cylindrical shells were used as the scattering medium, thus, these related investigations could be used only as references and occasional guides.



### III. SCOPE OF INVESTIGATION

The scattering of neutrons and gamma rays by thin cylindrical shells was investigated analytically and an attempt was made to verify these results by experimental means. The analytical investigation was made for point sources of radiation and finite size detectors, with the source positioned vertically below the center of the detector and with the center line of the detector coincident with the center line of the cylindrical shell.

Experimentally, the scattering of neutrons and gamma rays by 24ST and Alclad 24ST aluminum alloy cylindrical shells was investigated. However, the experimental results were overshadowed by the relatively large statistical deviations that were introduced when correcting the experimental readings for the scattering of the radiation by the air and the room.

Attempts to reduce this extraneous scattering to an acceptable level were unsuccessful. Thus, the experimental results with the exception of a few of the gamma ray readings neither proved or disproved the analytical findings. The few exceptions noted only tended toward support of the analytical results and no positive conclusions could be drawn.



## IV. SCATTERING FORMULAS

## A. Assumptions

The theoretical analysis of this problem concerning similitude in neutron and gamma ray scattering would have been extremely complicated without certain simplifying assumptions. These included the following.

It was assumed that the sources of radiation were point sources and that the neutrons or gamma rays were emitted isotropically. This is a valid assumption for very small finite sources. If the finite source cannot be considered very small, but is still small compared to the size of the scattering material, it can be approximated by a series of point sources.

Any scattering or absorption of neutrons or attenuation of gamma rays by the air was assumed to be negligible. That this is a valid assumption for neutrons follows from the magnitude of the probability that a neutron will be scattered or absorbed in air. The probability that a neutron will penetrate the air or other material a distance  $x$  without being scattered or absorbed is  $e^{-\Sigma x}$  where  $\Sigma$  is the macroscopic cross section for the event in question.

For a substance composed of more than one element  $\Sigma$  is calculated by using the formula

$$\Sigma = \rho \sum_{i=1}^n \frac{f_i \sigma_i}{A_i} \quad (1)$$



where

$\rho$  is the density of the substance

$N$  is Avogadro's number

$f_i$  is the weight fraction of the  $i$ th element  
of the substance

$\sigma_i$  is the microscopic cross section of the  $i$ th  
element for the event in question

$A_i$  is the atomic weight of the  $i$ th element.

For air at standard conditions, the value of  $\Sigma_s$  (scattering cross section) as calculated with this equation is  $4.5 \times 10^{-4} \text{ cm.}^{-1}$  and the value of  $\Sigma_a$  (absorption cross section) is  $7.2 \times 10^{-5} \text{ cm.}^{-1}$ .

The maximum neutron path length from the source to the detector in this experiment was approximately 65 cm. Thus, the probability that a neutron would be scattered by the air in this experiment was about 0.03 for the maximum distance and considerably less than this for the minimum distance. The probability that a neutron would be absorbed was approximately 0.005 for the maximum distance. These probabilities are for thermal neutrons. As the neutron energy increases  $\Sigma_s$  remains about constant and  $\Sigma_a$  is reduced considerably, so the absorption probability will be less than 0.005 for higher energy neutrons.

That the attenuation of gamma rays by air is very small can be seen by applying the factor  $e^{-\mu x}$  which is the probability that a gamma ray will penetrate a distance  $x$  into a medium without being involved in any reaction that contributes to its attenuation. The total absorption coefficient  $\mu$  is the sum of the absorption coefficients for photoelectric effect, Compton scattering, and pair production. For air,  $\mu$





varies between approximately  $1 \times 10^{-4} \text{ cm.}^{-1}$  for 0.1 Mev gamma rays and  $0.40 \times 10^{-4} \text{ cm.}^{-1}$  for 4 Mev gamma rays (1). Therefore, the probability that a gamma ray within this energy range would be attenuated by the air was about 0.0005 to 0.0026 for the maximum distance involved in this experiment.

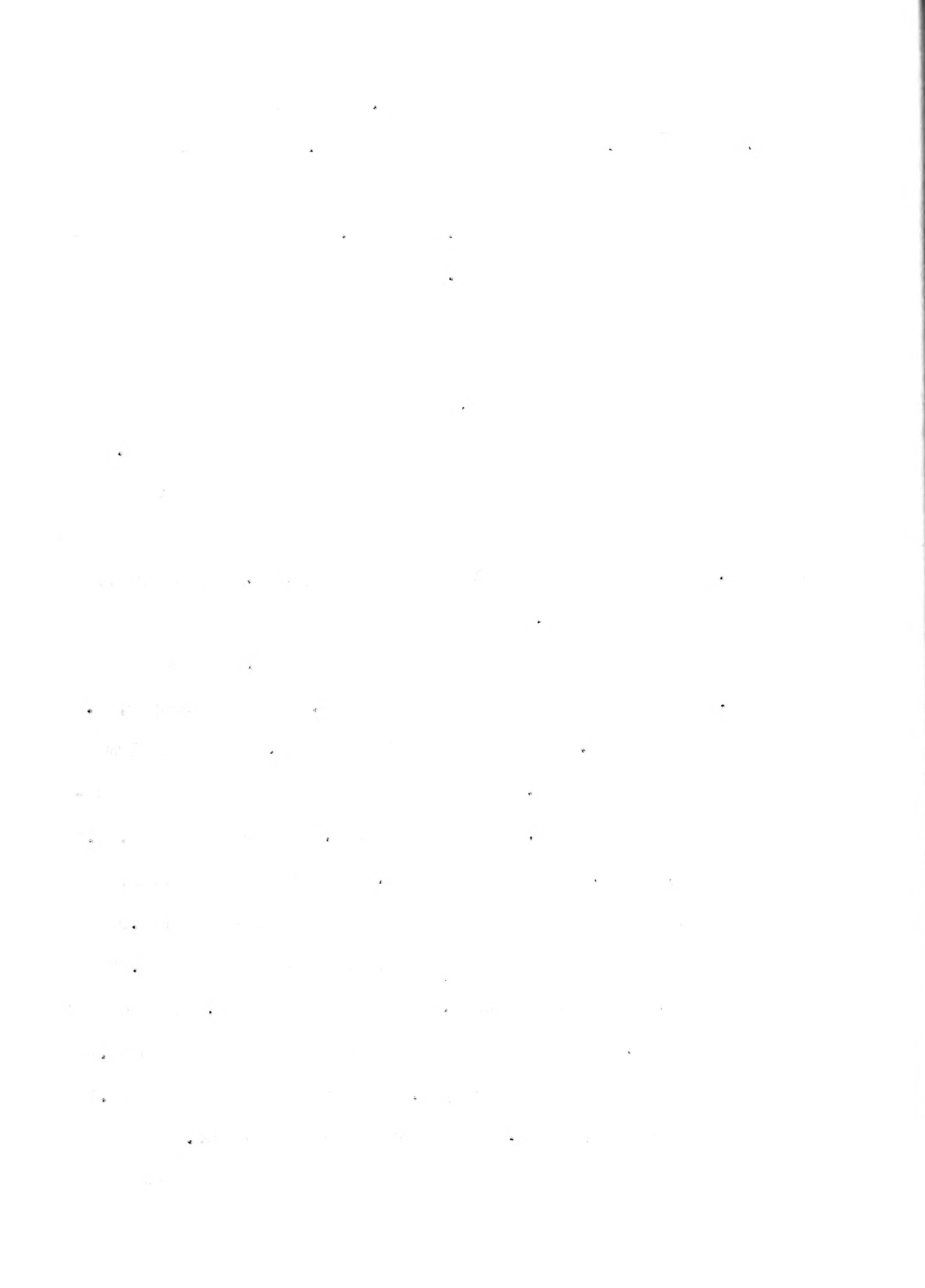
Another assumption used concerned the number of scattering collisions undergone by each neutron in the 245T aluminum or Alclad 245T aluminum cylindrical shells. It was assumed that each neutron that was scattered was involved in only one scattering collision. A consideration of the mean free path for neutron scattering  $\lambda_s$  in 245T aluminum alloy or Alclad 245T aluminum alloy shows that this assumption is valid. The mean free path  $\lambda_s$  is equal to  $1/\Sigma_s$ . Equation (1) was evaluated to find  $\Sigma_s$ .

The density of 245T wrought aluminum alloy is 2.77 grams per cubic cm. and its nominal composition (2) is 4.5 per cent copper, 0.6 per cent manganese, 1.5 per cent magnesium, and 93.4 per cent aluminum with its normal impurities. These normal impurities and the permissible maximum of each are 0.5 per cent iron, 0.1 per cent silicon, 0.1 per cent zinc, and 0.1 per cent chromium. The cladding metal, which is nominally 5 per cent of the total thickness of sheet 0.004 inch or over in thickness and 15 per cent for sheet less than 0.004 inch thickness, has a density of 2.71 grams per cubic cm. Its nominal composition is 99.3 per cent minimum aluminum with impurities of 0.7 per cent maximum iron plus silicon, 0.1 per cent maximum copper, 0.1 per cent maximum zinc, and 0.05 per cent maximum manganese.

Assuming that the amount of the impurities present is one-half







of the material,  $\Sigma_s$  for thermal neutrons for this alloy is  $0.0213 \text{ cm.}^{-1}$  and  $\Sigma_s$  for the cladding is  $1.965 \text{ cm.}^{-1}$ . Thus  $\lambda_s$ , which like  $\Sigma_s$  remains approximately constant with increasing neutron energy, is  $46.6 \text{ cm.}$  for the alloy and  $11.76 \text{ cm.}$  for the cladding. These values when compared with the maximum effective thickness of the material considered in this experiment, which is about  $0.62 \text{ cm.}$ , show that the assumption of only one collision for each neutron scattered should not have introduced any great error.

The scattering was assumed to be spherically symmetrical which would only be true if the mass of the scattering nucleus was much larger than the mass of the neutron. A measure of the anisotropy of the neutron scattering is the average cosine of the scattering angle in the laboratory system. Chadwick and Kurland (7, p. 27) show that this average cosine for neutrons with energies less than a few Mev is given by the equation

$$\overline{\cos \psi} = \frac{2}{3A}$$

where  $A$  is the mass number of the scattering material. The mass number of 2431 aluminum alloy, which is the sum of the weighted mass numbers of the constituents, is  $27.89$ . The mass number of the cladding computed in a similar manner is  $27.10$ . Thus,  $\overline{\cos \psi}$  is  $0.0231$  for the alloy and  $0.0246$  for the cladding. This indicates that the anisotropy is relatively low.

The slowing down of fast neutrons in the cladding can be taken to



elastic scattering of the neutrons upon collision with nuclei of the moderator, therefore, it was assumed that all the collisions in the scattering material were elastic.

Throughout the entire development, the absorption cross section was assumed to be small compared with the scattering cross section. Actually, since the absorption cross section for most elements decreases fairly rapidly with increasing neutron energy, this assumption would be of little concern in the design of shielding that must protect personnel from structurally scattered neutrons. Any shield that would protect them from fast neutrons would be effective against slow neutrons. Therefore, only calculations for fast neutron scattering would be necessary and in this energy range the absorption cross section is, with few exceptions, much smaller than the scattering cross section.

If for some reason the number of scattered slow neutrons must be known, this can be estimated quite accurately by slightly modifying the equation developed for fast neutrons. This modification is given at the end of the development of the fast neutron scattering equation.

The mean free path for neutron scattering  $\lambda_s$  is actually a function of energy. If the source of neutrons is not monoenergetic, this introduces another variable. However,  $\lambda_s$  is practically a constant for neutrons up to about 6 or 10 Mev and, therefore, it was assumed that a constant value could be used for a polyenergetic source of neutrons.





The differential cross section  $d\sigma/d\Omega$  for monoenergetic gamma ray scattering is a function of the angle of scattering. However, calculations show (5) that this is practically constant for angles of scattering greater than about 70 degrees. In this investigation, the angle of scattering, with few exceptions, was greater than this, thus a constant value was assumed for  $d\sigma/d\Omega$ .

### B. Neutron Scattering

Figure 1 is a sketch of the system investigated. The scattering material comprises a cylindrical shell of radius  $r$ , thickness  $t$ , and height  $h_1$ , one-quarter of which is shown. The counting tube with an active volume of radius  $a$  and height  $h_2$  and the point source are positioned on the center line of the cylindrical shell with the center line of the counting tube coincident with that of the shell. The top of the active volume of the vertically suspended counting tube is on the same horizontal level as the top edge of the scattering material. The point source is located on a horizontal line which is a distance  $h_3$  from the top edge of the scattering material and a distance  $h_1$  from the bottom edge.

The equation which gives the number of neutrons that are singly scattered by the cylindrical shell into the counting tube was developed as follows.

The neutron flux  $\phi$  which reaches the element of volume at  $P$  a distance  $r_1$  from the source (Figure 1) is



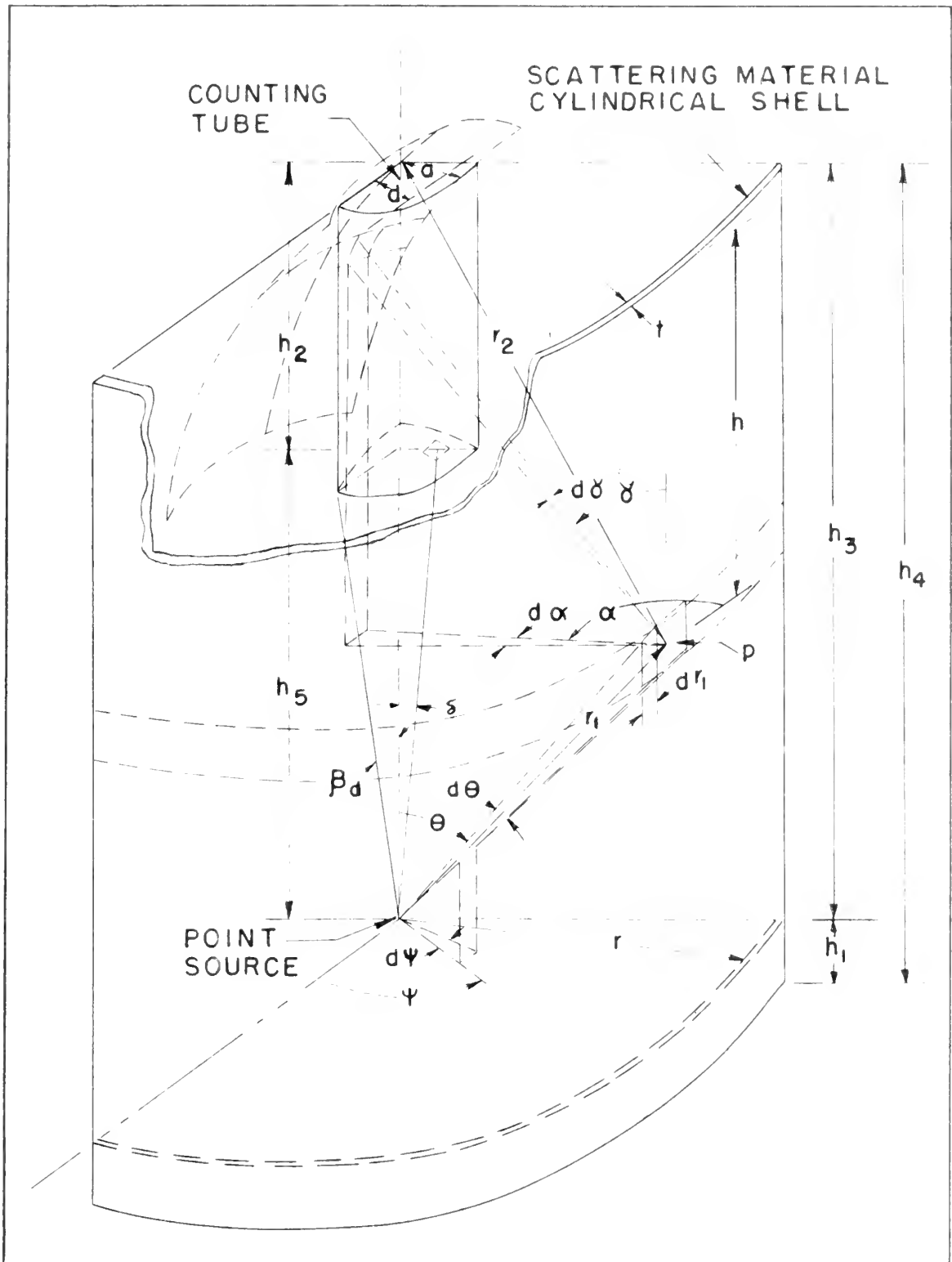


Figure 1. Geometry of scattering.



$$\phi = \frac{q}{4\pi r_1^2} \quad (2)$$

where  $q$  is the source strength in neutrons per second.

The effective volume element at  $P$  normal to the path of a radially emitted neutron is

$$dV = r_1^2 d\psi_1 d\theta_1 dr_1$$

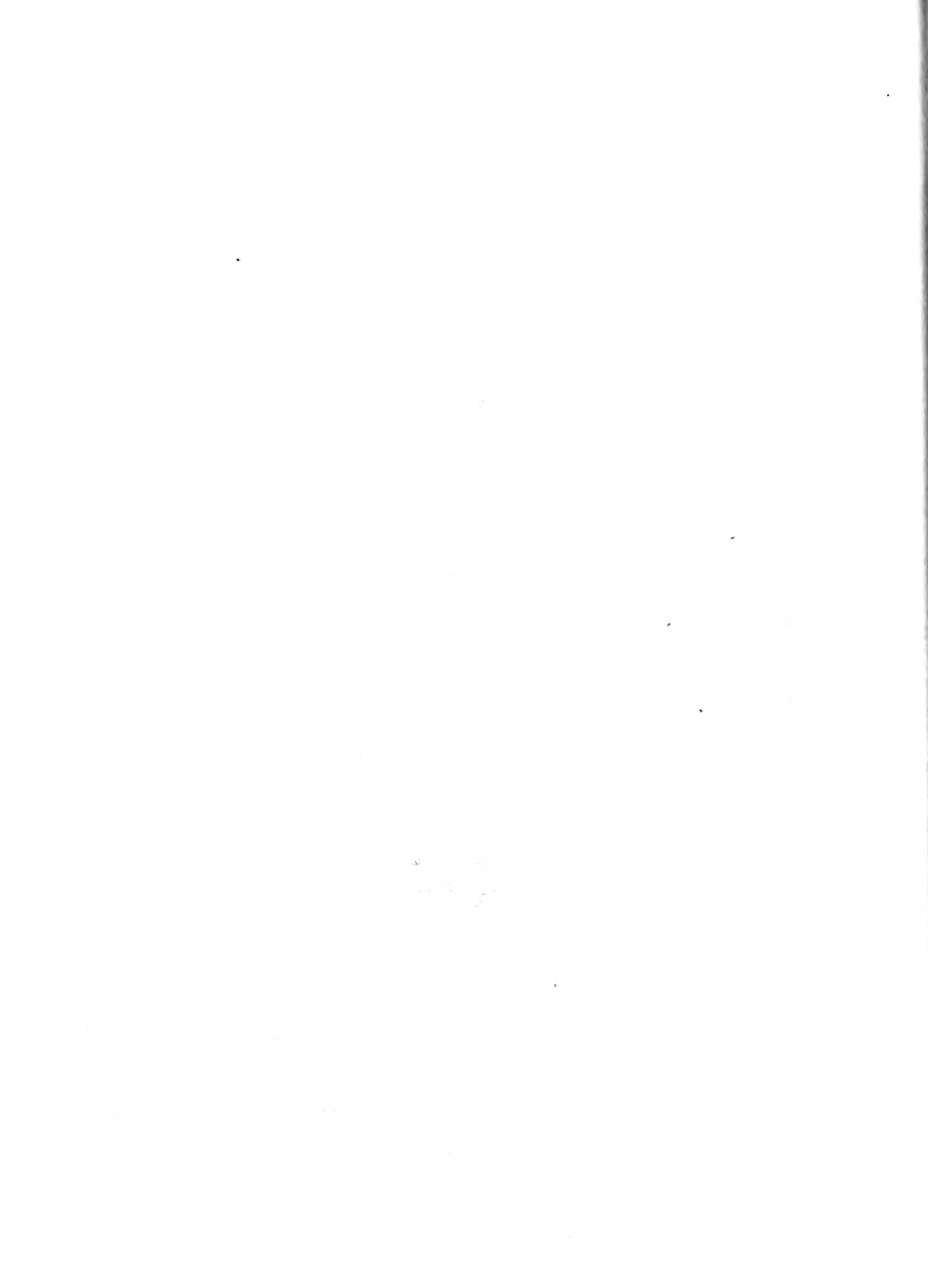
A radially emitted neutron travels a distance  $dr_1$  within this volume element. To determine the probability of a neutron being scattered while traveling this distance, the mean free path for scattering

$\lambda_s$  was used. This, the reciprocal of the macroscopic scattering cross section  $\Sigma_s$ , is the average distance a neutron travels between collisions. Thus, the probability that a neutron will be scattered while traveling the distance  $dr_1$  is  $dr_1 / \lambda_s$  and the probability  $p$  that the neutron will be scattered within the volume element is

$$p = \frac{r_1^2 d\theta_1 dr_1 d\psi_1}{\lambda_s}$$

Therefore, the number of neutrons  $n$  which are singly scattered within this volume element, which is Equation (2) times  $p$ , is

$$dn = \frac{q}{4\pi\lambda_s} d\theta_1 dr_1 d\psi_1 \quad (3)$$



assuming isotropic and elastic scattering, the proportion of the scattered neutrons that are scattered toward a point detector is  $1/4\pi r_2^2$  where  $r_2$  is the distance from the volume element to the point detector. However, with the presence of the probe and the internal structure, the volume element could not be regarded as a point detector. Instead, the ratio of the solid angle  $\Omega$  subtended by the detector, as viewed from the element of volume, to the total solid angle of  $4\pi$  steradians will be used.

This solid angle can then be found by considering a spherical surface (see Figure 1) which passes through the center of the top of the counting tube and is generated by revolving an arc of radius  $r_2$  centered at the volume element. The boundaries of the proper limits on  $\alpha$  and  $\gamma$ , the solid angle subtended by the counting tube can be determined.

The solid angle  $\Omega$  is

$$\Omega = \int_{\alpha_1}^{\alpha_2} \int_{\gamma_1}^{\gamma_2} \sin \gamma \, d\gamma \, d\alpha \quad (4)$$

where  $\alpha_1$  and  $\alpha_2$  are, respectively, minimum and maximum.

The limits on  $\alpha$  and  $\gamma$  are independent in a rather complicated way due to the shape of the counting tube. To avoid this complication and for convenience of calculation, the following approximation of  $\Omega$ , the limits on  $\alpha$  are set at





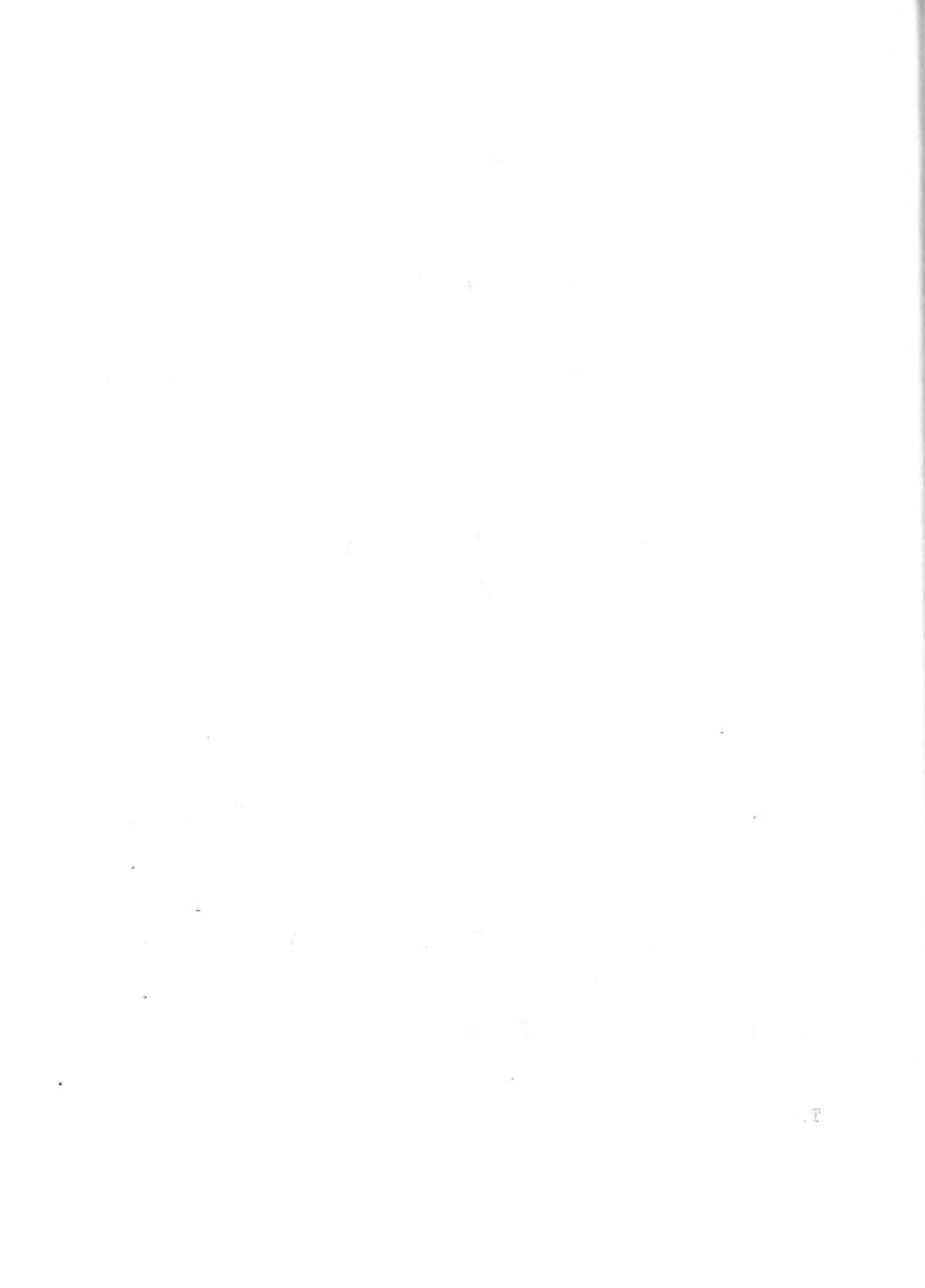
$$\alpha_1 = -\frac{\pi}{2} - \tan^{-1} \frac{a}{h_1}$$

$$\alpha_2 = -\frac{\pi}{2} + \tan^{-1} \frac{a}{h_2}$$

These limits on  $\alpha$  are independent of the other angles, thus, Equation (4) becomes upon integration over  $\alpha$  and substitution of these limits

$$\Omega = 2 \tan^{-1} \frac{a}{r} \int_{\gamma_1}^{\gamma_2} \sin \gamma \, d\gamma \quad (5)$$

Setting the limits on  $\gamma$  was not as simple a task as it first appeared. For instance, if  $\gamma_1$  is taken to be  $\cot^{-1} r/a$ , part of the upper extremities of the counting tube would be excluded from the solid angle. On the other hand, if  $\gamma_1$  is taken to be  $\cot^{-1} (r-a)/a$ , the solid angle would include some volume outside the counting tube. The same reasoning would apply to  $\gamma_2$  when  $h$  is less than  $h_2$ . When  $h$  is greater than  $h_2$ , a value of  $\cot^{-1} (h-h_2)/r$  for  $\gamma_2$  would not include all the bottom surface of the counting tube in the solid angle. As a compromise, the limits on  $\gamma$  were taken in two parts and were set by using the distance  $r$  minus  $d$ , where  $d$  is the mean integrated semi-chord. This is found from the equation



$$d = \frac{\int_{x=a}^{x=a} \sqrt{a^2 - x^2} \, dx}{2a}$$

Thus

$$d = \frac{\pi}{4} a$$

Then the limits are

$$\gamma_1 = \cot^{-1} \frac{h}{r+d} \quad (\text{all } h) \quad (6)$$

$$\gamma_{21} = \cot^{-1} \frac{h-h_2}{r+d} \quad (h \leq h_2) \quad (7)$$

$$\gamma_{22} = \cot^{-1} \frac{h-h_2}{r+d} \quad (h \geq h_2) \quad (8)$$

The contribution of the bottom of the detector to the solid angle is included by making the denominator of the latter limit  $r+d$ .

These limits on  $\gamma$  are independent of  $\psi$ , but are dependent on  $\theta$  being related through  $h$  by the equation

$$h = h_2 - r \cot \theta \quad (9)$$

Equation (5) gives the solid angle subtended by the counting tube. This divided by the total solid angle  $4\pi$  steradians is the proportion of prompt fission neutrons that will pass through the counting tube volume.



The number of neutrons scattered within the volume element is given by Equation (3), thus, this times the above ratio is the number of neutrons  $n_s$  that are scattered into the counting tube by the volume element. So

$$\int_0^{n_s} dn_s = \int_V \left[ \frac{Q}{16 \pi^2 \lambda_s} \left[ 2 \tan^{-1} \frac{a}{r} \int_{\gamma_1}^{\gamma_2} \sin \gamma d\gamma \right] d\theta dr_1 d\psi \right]$$

The limits on  $\psi$  are zero and  $2\pi$  and the limits on  $r_1$  are  $r/\sin\theta$  and  $(r+t)/\sin\theta$  where  $t$  is the perpendicular thickness of the scattering material. Integrating over  $r_1$  and  $\psi$  and substituting the limits give

$$n_s = \frac{Qt}{6 \pi \lambda_s} \int_{\theta_1}^{\theta_2} \left[ 2 \tan^{-1} \frac{a}{r} \int_{\gamma_1}^{\gamma_2} \sin \gamma d\gamma \right] \frac{d\theta}{\sin \theta} \quad (10)$$

Integrating in this equation over  $\gamma$  and substituting the limits (Equations (6), (7), and (8)) and then substituting for  $h$  from Equation (9) result in an extremely complicated and lengthy integral of  $\theta$ . To arrive at a simpler but still a good approximate expression for  $n_s$ , the bracket of Equation (10) which is the integral equation for  $n$  was replaced by the average value of  $n$ . This average value is found as follows.

Equation (5) is integrated over the limits as given by Equations (6),

2

(7), and (8) are substituted. This gives

$$\alpha = 2 \tan^{-1} \frac{a}{r} \left[ \frac{h_2 - h}{\sqrt{(h - h_2)^2 + (r - d)^2}} + \frac{h}{\sqrt{h^2 + (r - d)^2}} \right] \quad (h \leq h_2) \quad (11)$$

$$\alpha = 2 \tan^{-1} \frac{a}{r} \left[ \frac{h_2 - h}{\sqrt{(h - h_2)^2 + (r + d)^2}} + \frac{h}{\sqrt{h^2 + (r - d)^2}} \right] \quad (h \geq h_2) \quad (12)$$

The values of  $\alpha$  throughout the range of  $h$  are found for the geometry involved by assigning values to  $h$ , say  $n_0, n_1, n_2, \dots, n_1 \dots h_4$ . These values run from zero to  $h_2$  (Figure 1) and are equally spaced, the distance between them being  $b$ . Then the average value of  $\alpha$ , say  $\bar{\alpha}$ , is found from the equation

$$\bar{\alpha} = \frac{\sum_{i=0}^{i=(h_2/b)-1} \frac{\alpha_i + \alpha_{i+1}}{2}}{h_2/b} \quad (13)$$

Values of  $\bar{\alpha}$  for the various geometries used in this investigation are plotted in Figure 2.

Using this average value of  $\alpha$ , Equation (10) can be written

$$n_s = \frac{it \bar{\alpha}}{c \pi \lambda_s} \int_{\theta_1}^{\theta_2} \frac{d\theta}{\sin \theta} \quad (14)$$

1. The first part of the paper is devoted to the study of the properties of the function  $f(x)$  defined by the equation

$$f(x) = \int_0^x \frac{1}{1+t^2} dt$$

It is well known that the function  $f(x)$  is increasing and concave down on the interval  $(-\infty, \infty)$ . The function  $f(x)$  is also bounded on the interval  $(-\infty, \infty)$ .

2. The second part of the paper is devoted to the study of the properties of the function  $g(x)$  defined by the equation

$$g(x) = \int_0^x \frac{1}{1+t^4} dt$$

It is well known that the function  $g(x)$  is increasing and concave down on the interval  $(-\infty, \infty)$ . The function  $g(x)$  is also bounded on the interval  $(-\infty, \infty)$ .



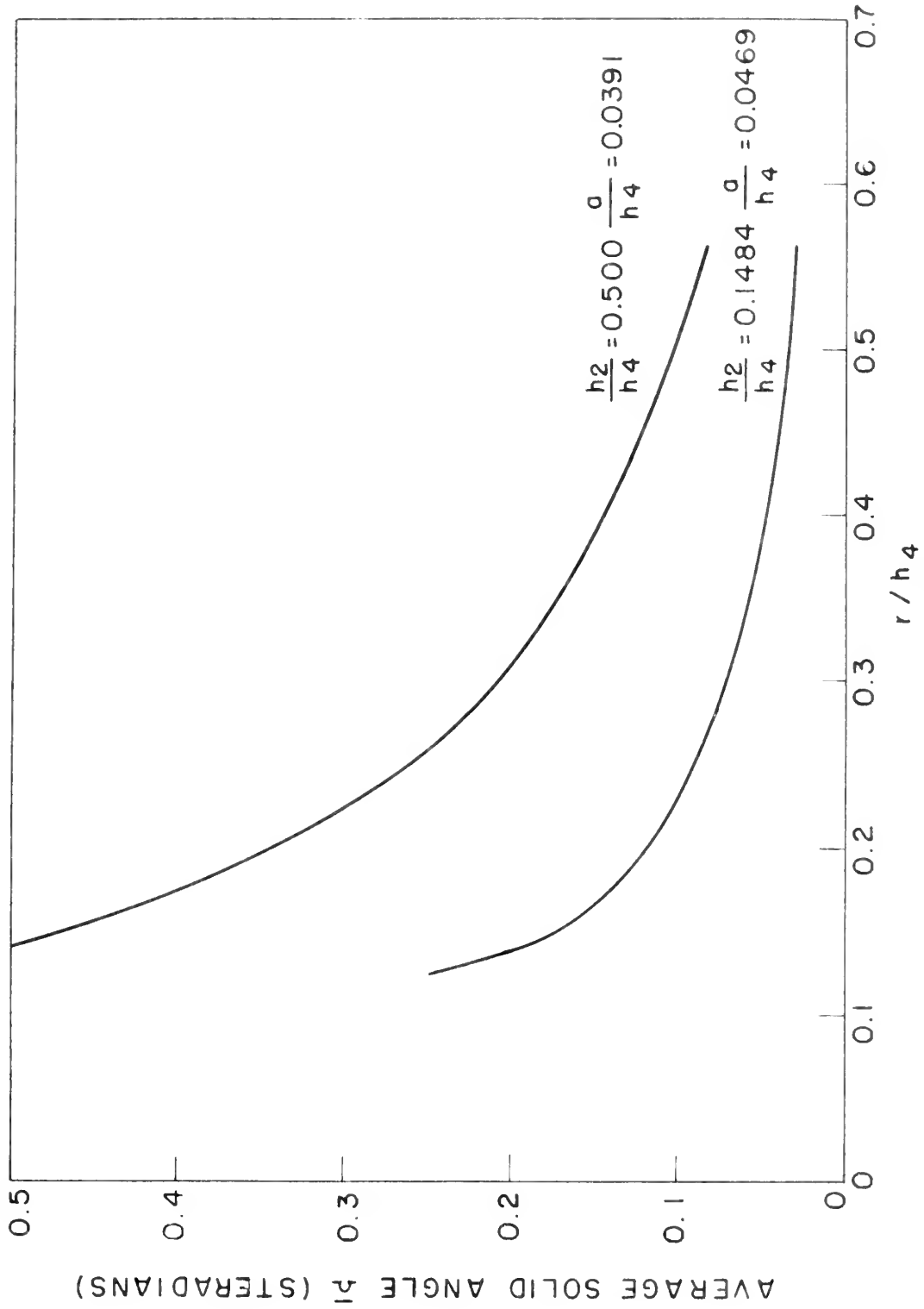


Figure 2. Average solid angle for various geometries.



From Figure 1, it is seen that the limits on  $\theta$  are

$$\theta_1 = \cot^{-1} \frac{h_3}{r}$$

$$\theta_2 = \cot^{-1} \frac{h_1}{r}$$

where  $h_1$  is considered positive if the bottom edge of the cylindrical shell is horizontally above the source and negative if the bottom edge is below the source.

The integration of equation (1b) and substitution of the limits gives

$$u_s = \frac{q \bar{a} t}{8 \pi \lambda_s} \left[ \ln \left( \sqrt{1 + \left( \frac{h_1}{r} \right)^2} - \frac{h_1}{r} \right) - \ln \left( \sqrt{1 + \left( \frac{h_3}{r} \right)^2} - \frac{h_3}{r} \right) \right]$$

Referring to Figure 1, it is evident that  $h_1/r$  is the tangent of the backward angle at the source and  $h_3/r$  is the tangent of the forward angle. Thus the substitution of

$$\tan \beta_b = \frac{h_1}{r}$$

$$\tan \beta_f = \frac{h_3}{r}$$

$$\left[ \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} - \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} \right] \cdot \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$$

$$A = B$$

$$C = D$$

and combination of the natural log terms gives

$$n_s = \frac{Q \bar{n} t}{8 \pi \lambda_s} \ln \left[ \frac{\sqrt{1 + \tan^2 \beta_b} - \tan \beta_b}{\sqrt{1 + \tan^2 \beta_f} - \tan \beta_f} \right]$$

Now

$$\sqrt{1 + \tan^2 \beta_b} = \frac{1}{\cos \beta_b}$$

and

$$\tan \beta_b = \frac{\sin \beta_b}{\cos \beta_b}$$

so that the numerator of the natural log in the above equation can be written  $(1 - \sin \beta_b)/\cos \beta_b$ . A similar expression can be substituted for the denominator to give

$$n_s = \frac{Q \bar{n} t}{8 \pi \lambda_s} \ln \left[ \left( \frac{1 - \sin \beta_b}{\cos \beta_b} \right) \left( \frac{\cos \beta_f}{1 - \sin \beta_f} \right) \right]$$

The final expression for  $n_s$  is found by letting

$$n = \ln \left[ \left( \frac{1 - \sin \beta_b}{\cos \beta_b} \right) \left( \frac{\cos \beta_f}{1 - \sin \beta_f} \right) \right]$$



so that

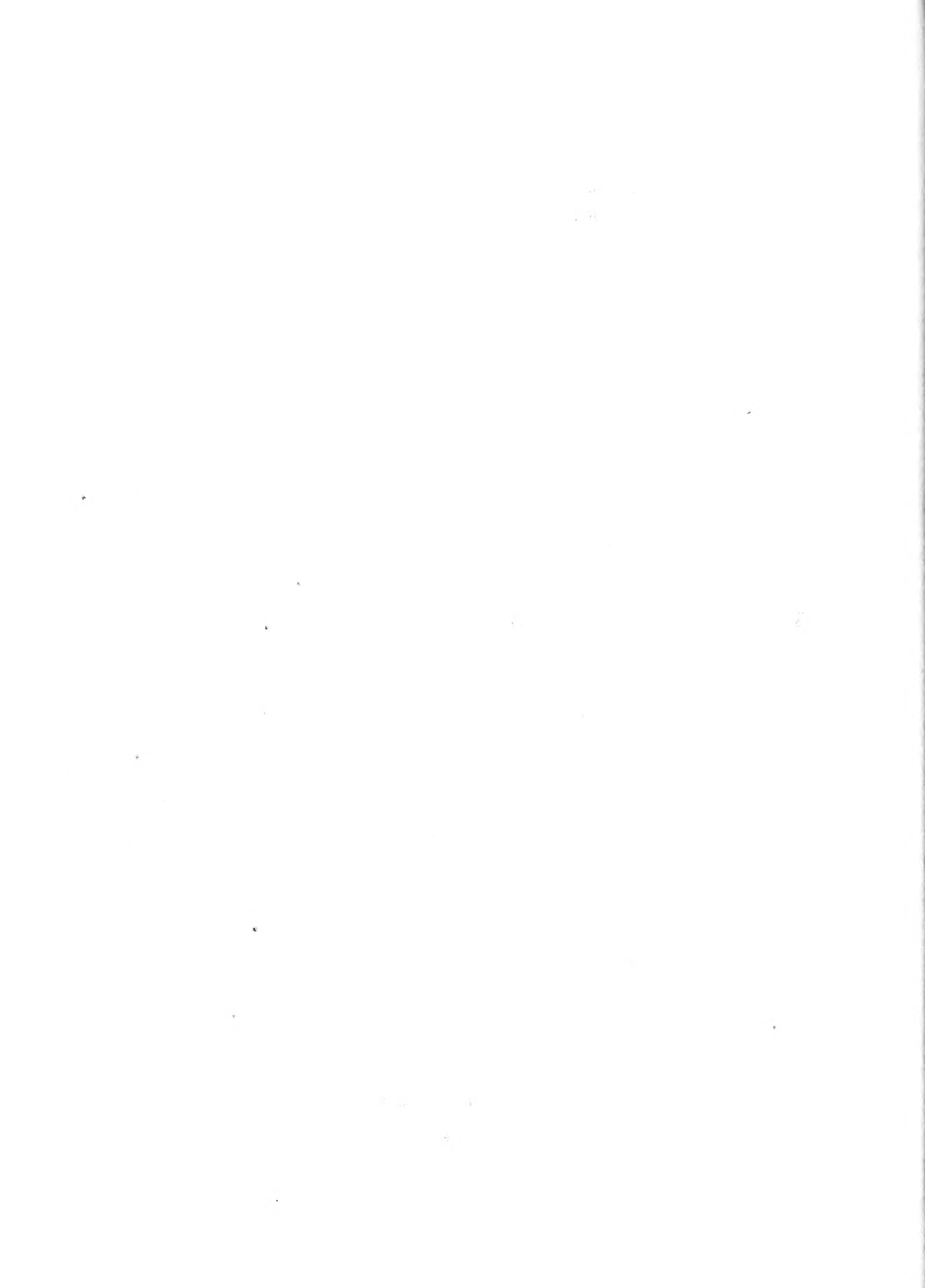
$$n_0 = \frac{\pi a^2 H}{\pi \lambda_s} \quad (15)$$

is a measure of the total number of neutrons per second that are singly scattered by the cylindrical shell into the conical tube volume. When evaluating  $H$ , it must be remembered that  $H$  is considered positive if the bottom edge of the cylindrical shell is horizontally above the source and negative if the bottom edge is below the source. Therefore,  $\beta$  and, consequently,  $\sin \beta$  are positive for the first mentioned conditions and negative for the latter. A plot of  $H$  versus  $\beta$  for various values of  $\beta$  is given in Figure 3.

For a polyenergetic neutron source, Equation (15) can represent the total number of fast neutrons that are singly scattered if  $\lambda$  is replaced by the fast neutron mean free path emitted by the source. A possibility for the need of a slight modification to this equation arises from the fact that a small fraction of the fast neutrons emitted at energies just above thermal are reduced to thermal energies upon colliding with the nuclei of the moderating material.

The energy  $E'$  of these neutrons after the collision is related to the energy  $E$  before the collision by the formula (7, p. 140)

$$E' = E \frac{A+1}{A+1} \epsilon + 1$$





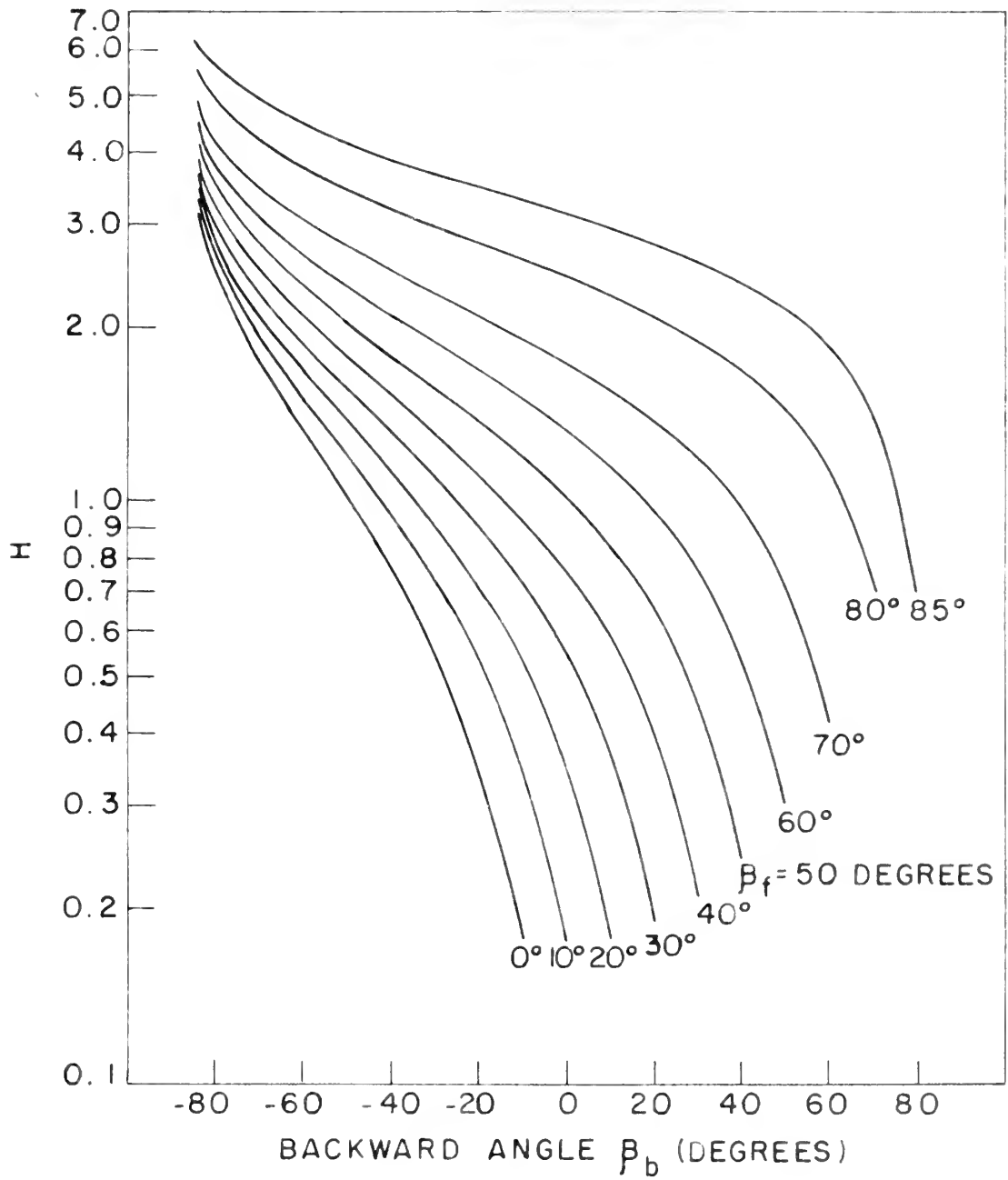
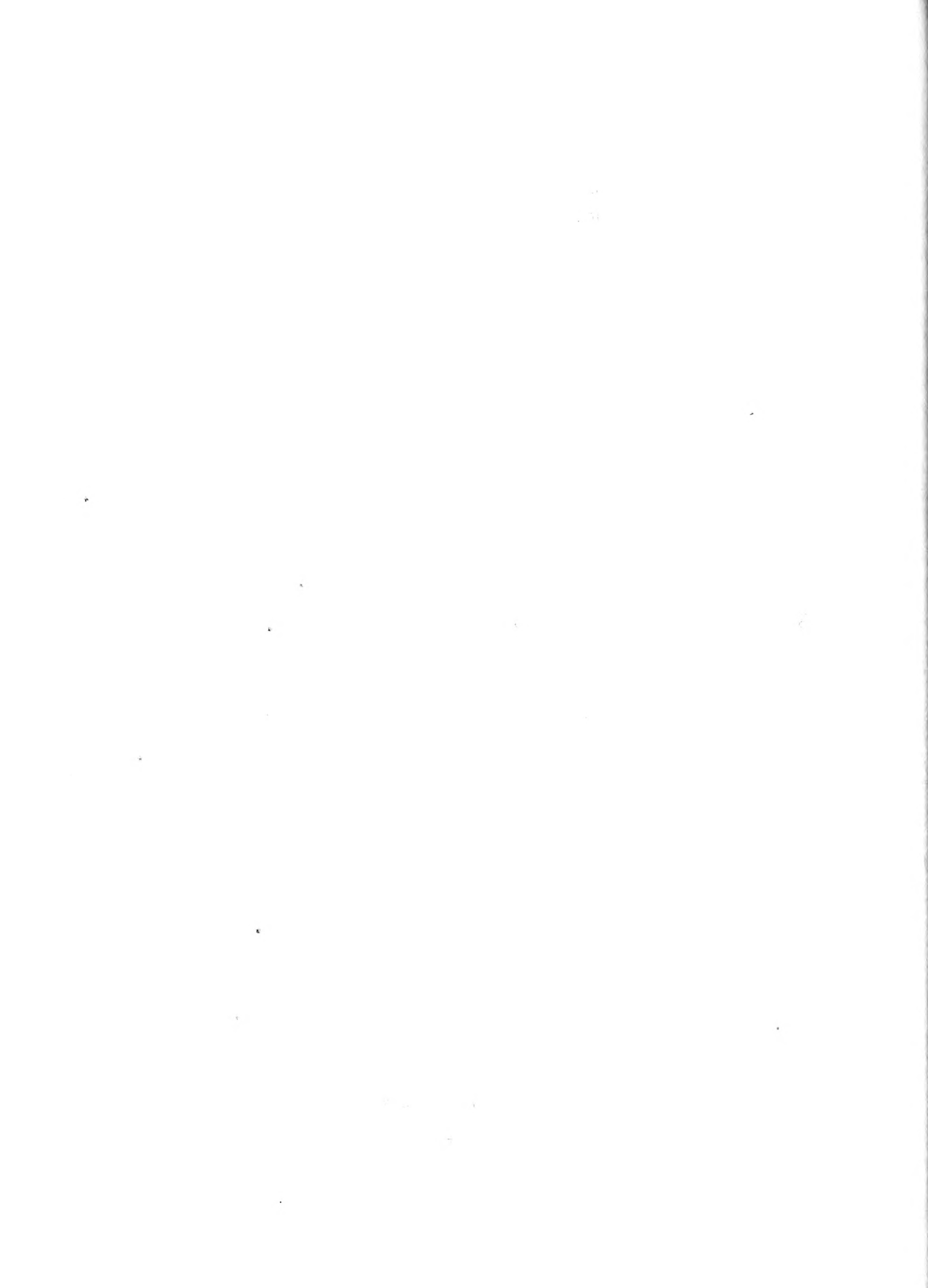


Figure 3. Variation of  $H$  with geometry.



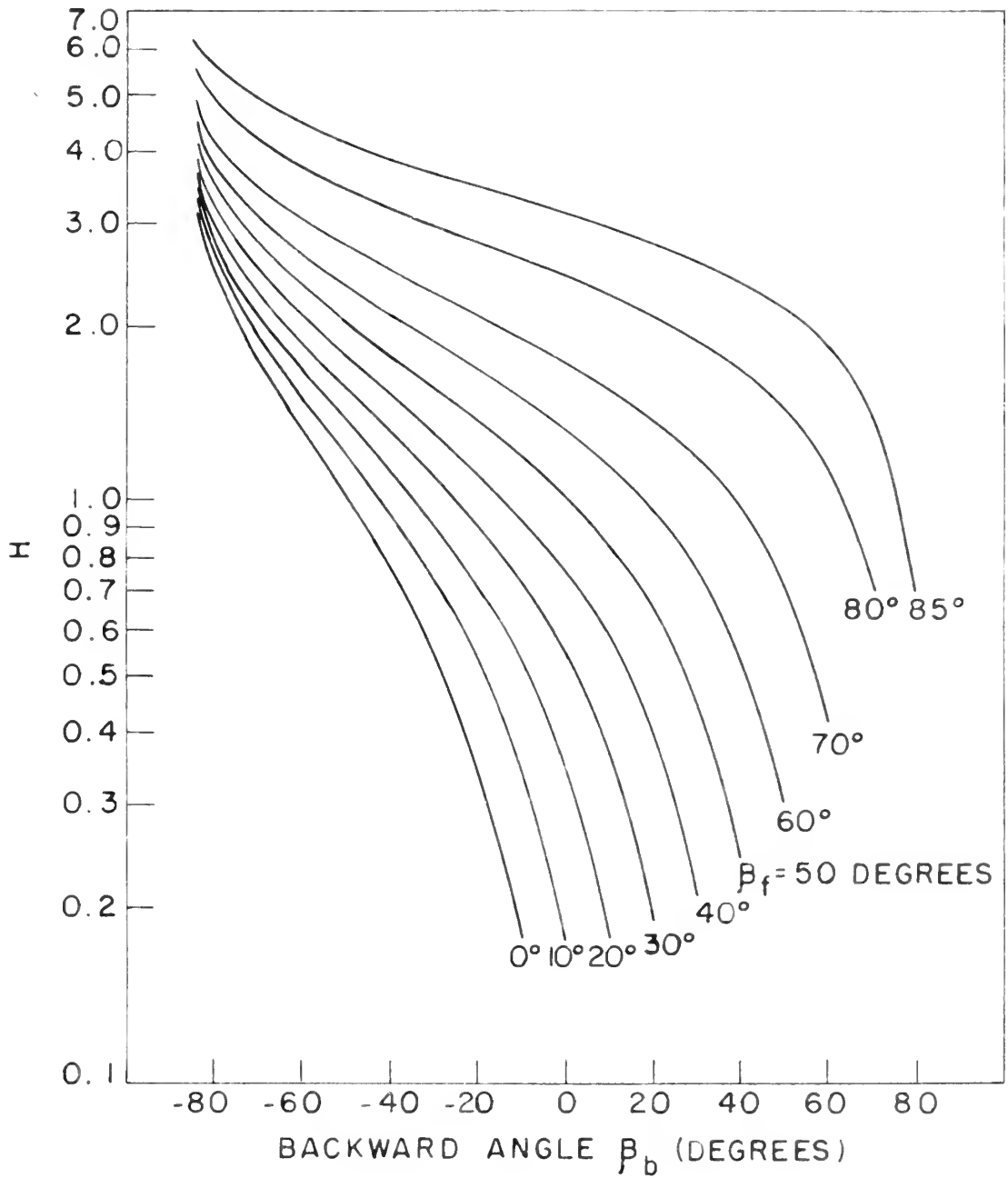


Figure 3. Variation of  $H$  with geometry.

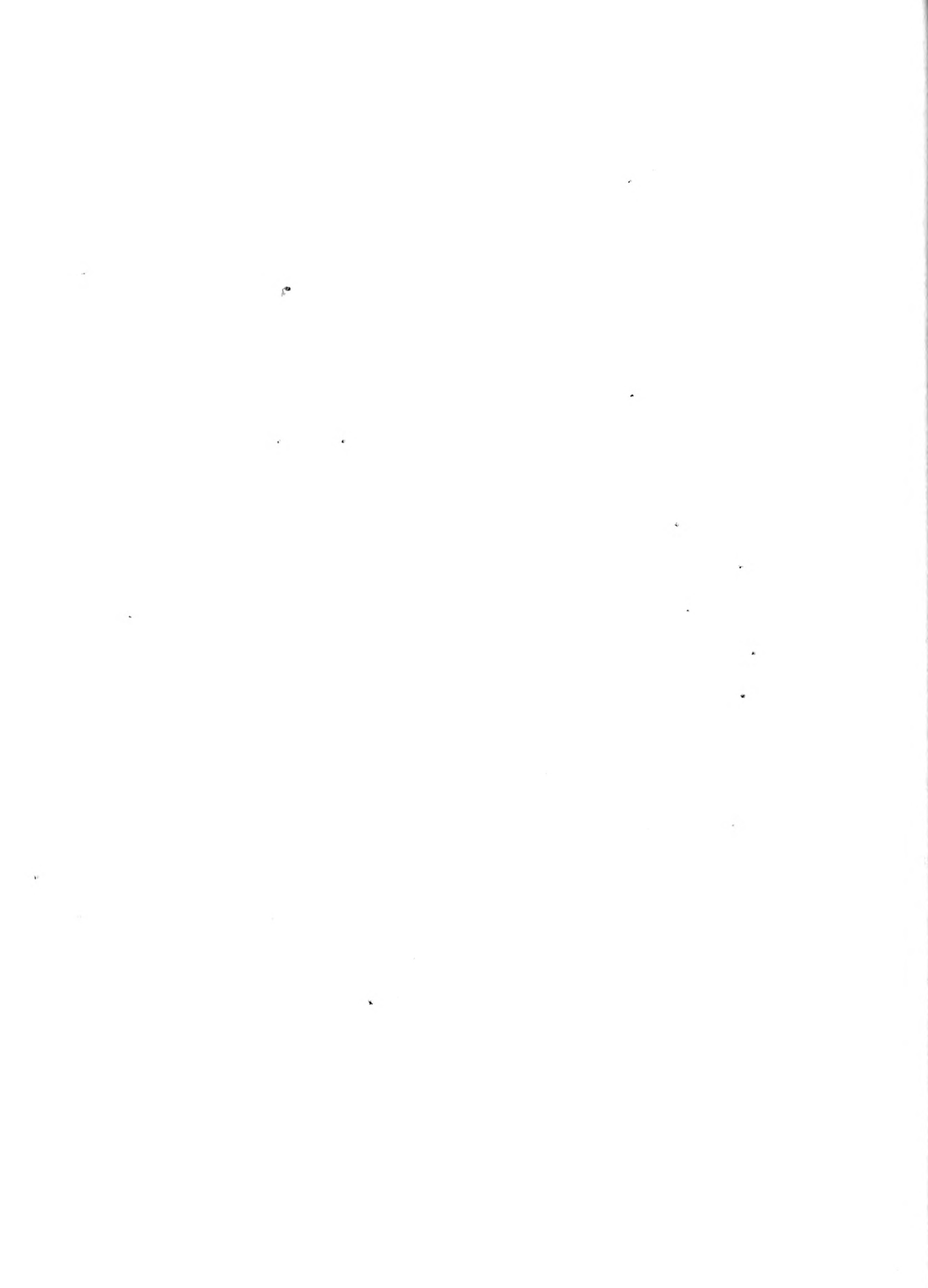


where  $A$  is the mass number of the scattering material and  $\epsilon$  is the scattering angle. Since the neutrons of interest here are those scattered into the thermal energy region, the energy after collision is  $E_t$  where  $E_t$  is the defined maximum energy of thermal neutrons.

In this investigation or in similar setups with shells of structural material, the scattering angle has an average value of about 70 degrees. For this scattering angle and 2024 aluminum alloy  $H'$ , using the above equation, is equal to 0.935  $E_t$ . Thus, on the average, those neutrons emitted by the polychromatic source in the energy range from  $E_t$  to 1.07  $E_t$  are scattered into the thermal neutron energy region. For example, if thermal neutrons are defined as those with an energy of 0.25 ev or less, the neutrons with energies between 0.25 and 0.268 ev are scattered upon collision into the thermal energy region.

For almost all neutron sources, the number of neutrons emitted in this very narrow energy band are a minute fraction of the total neutrons emitted. Hence, for practical purposes, all neutrons emitted as fast (slow) neutrons can still be considered as such after they are scattered. Thus, Equation (15) is applicable to fast neutrons, as are the subsequent equations given in this section, if  $Q$  is the number of fast neutrons per second emitted by the source.

Other measurements of the scattering by the cylindrical shells would be the ratio  $R_s$  of the neutrons scattered into the counting tube to those that reach the counting tube directly or the ratio  $R_t$  of the total neutrons that reach the counting tube to those that proceed



directly.

The number of neutrons that arrive directly is the point source strength  $Q$  times the ratio of the solid angle subtended by the end of the counting tube to the total solid angle  $4\pi$  steradians. The solid angle subtended by the bottom of the quarter of the detector shown on Figure 1 is

$$\Omega = \frac{\pi}{2} \int_{\delta_1}^{\delta_2} \sin \delta \, d\delta$$

The limits on  $\delta$  are zero and  $\cot^{-1} h_5/a$ , thus

$$\Omega = \frac{\pi}{2} \left( 1 - \frac{h_5^2}{\sqrt{h_5^2 + a^2}} \right)$$

The solid angle  $\Omega_d$  subtended by the bottom of the detector is four times this, or

$$\Omega_d = 2\pi \left( 1 - \frac{h_5^2}{\sqrt{h_5^2 + a^2}} \right)$$

The proportion of the source neutrons which arrive directly at the detector is  $\Omega_d/4\pi$ , so the number  $n_d$  of source neutrons that arrive directly is

$$n_d = \frac{Q}{2} \left( 1 - \frac{h_5^2}{\sqrt{h_5^2 + a^2}} \right)$$

The term in the parenthesis can be written as

$$1 - \frac{1}{\sqrt{1 + \left( \frac{a}{h_5} \right)^2}}$$

3-7

$$\frac{1}{\sqrt{1-x^2}}$$

$$\left( \frac{1}{\sqrt{1-x^2}} \right)'$$

$$\left( \frac{1}{\sqrt{1-x^2}} \right)'$$

$$\left( \frac{1}{\sqrt{1-x^2}} \right)'$$



where (see Figure 1)

$$\frac{a}{n_g} = \tan \beta_d$$

substituting from this relationship for  $a/n_g$  and then substituting  $1/\cos \beta_d$  for  $\sqrt{1 + \tan^2 \beta_d}$  gives the final expression for  $n_d$ . Thus,

$$n_d = \frac{1}{2} (1 - \cos \beta_d) \quad (16)$$

The scattering ratio  $R_s$  was previously defined as  $n_g/n_d$  (Equations (15) and (16)). So

$$R_s = \frac{\bar{n} \omega}{4 \pi \lambda_g (1 - \cos \beta_d)} \quad (17)$$

The total ratio  $R_T$  was previously defined as  $(n_g + n_d)/n_d$  which equals  $(n_g/n_d) + 1$ . Thus

$$R_T = R_s + 1 \quad (18)$$

Equations (17) and (18) can be applied to the total neutrons from a polynenergetic source or to the fast neutrons from a polynenergetic source or a monenergetic source. These equations can also be applied to thermal neutrons if the cross section for absorption is negligible compared to the cross section for scattering. Under similar circum-



sterious, Equation (15) can be used provided  $S$  is the thermal neutrons per second emitted by the source.

If the absorption cross section is not negligible compared to the scattering cross section, but is still somewhat less than the scattering cross section and, if the thickness of the cylindrical shells used is small compared to the mean free path for absorption (which it must be for Equation (15) to be valid), a good first approximation of the thermal neutron scattering can be calculated as follows.

The fraction of normally incident thermal neutrons that would be absorbed in the shell, if the scattering cross section were negligible, is  $(1 - e^{-\Sigma_a t})$  where  $\Sigma_a$  is the macroscopic absorption cross section and  $t$  is the thickness of the shell. This fraction times Equation (15) gives a good first approximation of the number  $n_{st}$  of thermal neutrons scattered by the cylindrical shell into the counter tube volume. Thus

$$n_{st} = \frac{S \bar{n} t \lambda_s}{5 \pi \lambda_s} \left( 1 - e^{-\Sigma_a t} \right) \quad (19)$$

Equations (17) and (19) are, for this case,

$$R_{st} = \frac{n_{st}}{n_{dt}} \quad (20)$$

and

$$R_{st} = R_{dt} + 1 \quad (21)$$



where  $n_{d_0}$  is defined by Equation (16) provided that  $q$  of the equation is the number of thermal neutrons per second emitted by the source.

### C. Gamma Ray Scattering

The geometry for gamma ray scattering is the same as that for neutron scattering (Figure 1) and the development of an equation for noncoherent gamma ray scattering is similar to the development of the equation for neutron scattering.

If it is assumed that no attenuation of the gamma rays occurs in the air, the gamma ray flux  $\phi_\gamma$  which reaches the element of volume at P at distance  $r_1$  from the source is

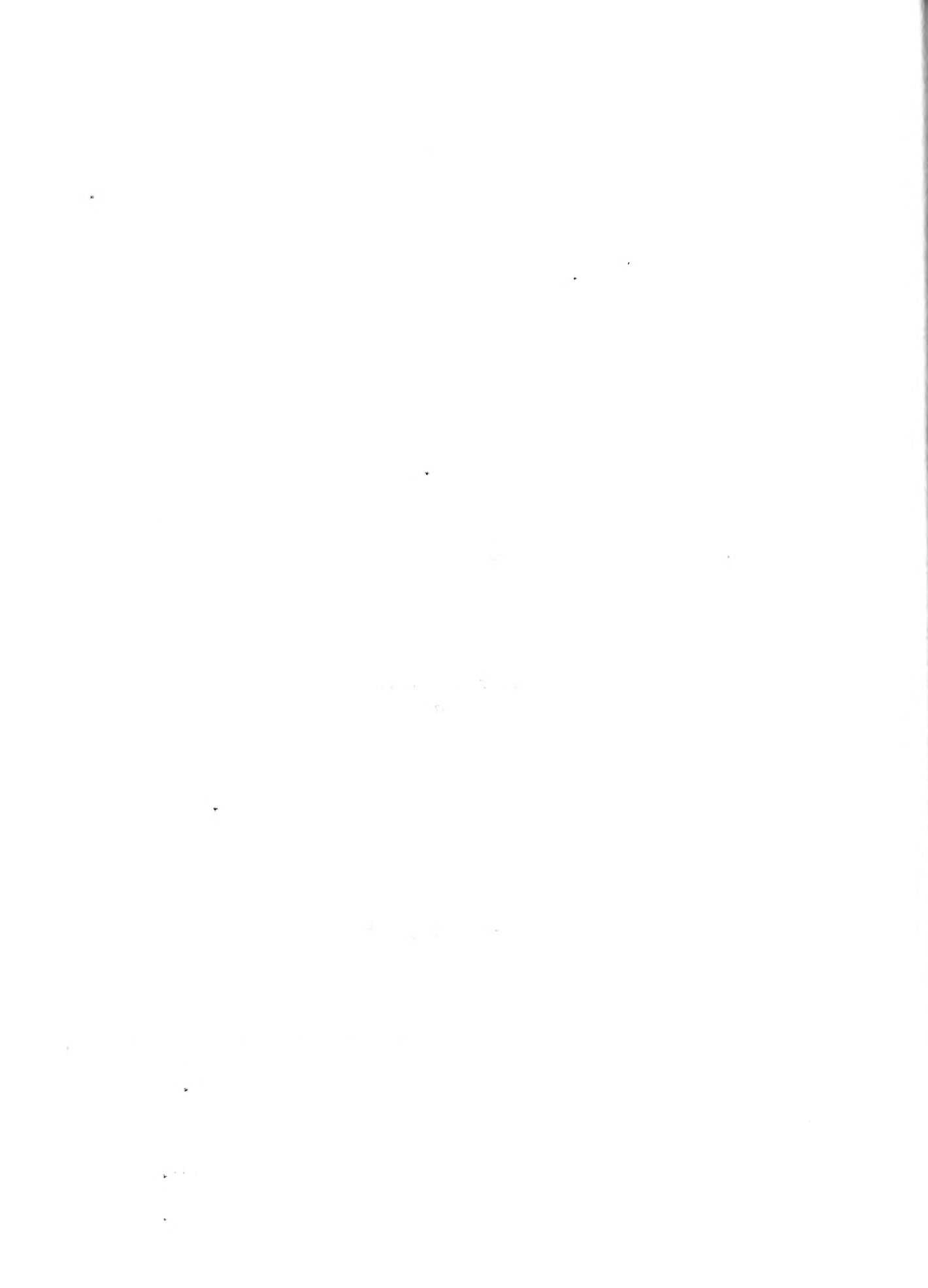
$$\phi_\gamma = \frac{S}{4\pi r_1^2}$$

where  $S$  is the source strength in gamma rays per second.

The effective volume element at P is

$$d = r_1^2 d\psi \sin\theta dr_1$$

The differential cross section  $d\sigma/d\Omega$  for gamma ray scattering, which has units cm.<sup>2</sup> per incident photon per electron cm.<sup>2</sup> per steradian, is the probability that a gamma ray will be scattered through an angle  $\epsilon$  into the element of solid angle centered about  $\epsilon$ . This cross section times the number of electrons  $n_e$  in a cube cm. of the



scattering material times the volume element gives the probability of a photon being singly scattered through the angle  $\epsilon$  into the element of solid angle centered about  $\epsilon$  while within the volume element.

Consequently, the number of gamma rays  $n_\gamma$  scattered while within the volume element is the flux at the element times the probability of scattering within the element, or

$$dn_\gamma = \frac{S}{4\pi} \frac{d\sigma}{d\Omega} n_0 d\theta d\psi dr_1$$

The number of gamma rays  $n_{g\gamma}$  which are scattered into the counting tube volume is the above equation multiplied by the solid angle subtended by the counting tube as seen from the volume element. This solid angle is given by Equation (4). To avoid the difficulties identical to those encountered in the neutron scattering, equation development, the solid angle subtended by the counting tube was replaced by the average angle  $\bar{\Omega}$ . Equations (11), (12) and (13) are used to calculate  $\bar{\Omega}$ . Values of  $\bar{\Omega}$  for the various geometries used in this investigation are plotted in Figure 2.

The number of gamma rays  $n_{g\gamma}$  which are scattered into the counting tube volume is found by multiplying the above equation by this average angle. Thus,

$$dn_{g\gamma} = \frac{S\bar{\Omega}}{4\pi} \frac{d\sigma}{d\Omega} n_0 d\theta d\psi dr_1$$





The differential cross section  $d\sigma/d\Omega$  which is a function of energy and the scattering angle is approximately constant for scattering angles greater than about 70 degrees. In this investigation and in similar setups with scattering material shells, the scattering angle is greater than 70 degrees except for shells with very small radii, thus,  $d\sigma/d\Omega$  was assumed to be constant. The number of electrons per cubic cm. is a constant for a particular scattering material. These constants can be taken outside the integral and the equation for  $n_{s\gamma}$  can be written

$$n_{s\gamma} = \frac{S \bar{n} n_e}{4\pi} \frac{d\sigma}{d\Omega} \int_{(r)_{11}}^{(r)_{12}} \int_{\psi_1}^{\psi_2} \int_{\theta_1}^{\theta_2} d\theta d\psi dr_1$$

where the subscripts 1 and 2 signify, respectively, minimum and maximum.

As in the neutron scattering equation development, the limits on  $r_1$ ,  $\psi$ , and  $\theta$  are

$$(r)_{11} = \frac{r}{\sin \theta}$$

$$(r)_{12} = \frac{r+t}{\sin \theta}$$

$$\psi_1 = 0$$



$$\psi_2 = 2\pi$$

$$\theta_1 = \cot^{-1} \frac{h_2}{r}$$

$$\theta_2 = \cot^{-1} \frac{h_1}{r}$$

In the latter limit,  $h_1$  is considered positive if the bottom edge of the cylindrical shell is horizontally above the source and negative if the bottom edge is below the source.

Integrating and applying these limits gives the expression for the number of monoenergetic gamma rays per second that are singly scattered into the counting tube volume. This expression is

$$n_{s\gamma} = \frac{S \bar{n} n_0 t}{2} \frac{d\sigma}{d\Omega} \left[ \ln \left( \sqrt{1 + \left( \frac{h_1}{r} \right)^2} - \frac{h_1}{r} \right) - \ln \left( \sqrt{1 + \left( \frac{h_2}{r} \right)^2} - \frac{h_2}{r} \right) \right]$$

The term within the brackets is  $\beta$  which was defined in the neutron scattering section development. A plot of  $\beta$  versus  $\beta_0$  for various values of  $\beta_1$  is given in Figure 3. Placing  $\beta$  in the above equation



gives

$$n_{S\gamma} = \frac{\pi n_0 \sin^2 \theta}{2} \frac{d\sigma}{d\Omega} \quad (22)$$

The ratios  $R_S$  and  $R_T$  were defined in the development of the equation for neutron scattering.  $R_S$  is  $n_S/n_d$  where  $n_d$  is the number of reactions that proceed directly from the source to the counting tube. This is given by Equation (16) with  $\theta$  replaced by  $\beta$ . Thus, for gamma rays,

$$R_{S\gamma} = \frac{\pi n_0 \sin^2 \theta}{(1 - \cos \beta_d)} \frac{d\sigma}{d\Omega} \quad (23)$$

and

$$R_{T\gamma} = R_{S\gamma} + 1 \quad (24)$$



## V. EXPERIMENTAL PROGRAM

### A. Materials

The materials used in this investigation were 2437 and Alclad 2437 aluminum alloy, paraffin, cadmium, lead, plywood, borated sand, a neutron source, and a gamma ray source.

The aluminum alloy was purchased from the Iowa State College Instrument Shop, the paraffin and plywood were purchased from local concerns, and the cadmium in the form of 0.010 inch sheet was purchased from the Division Lead Company, Summit, Illinois. The lead and borated sand were available in the laboratory.

A polonium-beryllium neutron source was used. This source is contained in two right cylinders. The outer cylinder has external dimensions of 1.0 inch diameter and 1.25 inches height. The dimensions of the inner cylinder, within which the source is sealed, were estimated by comparison with dimensions given by Rausa (1) for the same type of source. Thus, the inner right cylinder was estimated to have internal dimensions of 0.50 inch diameter and 0.40 inch height.

The strength of this source on April 9, 1953 was 3500 millicrouries, therefore, the strength at the time of the experiment (May 1954) was approximately 114 millicrouries. The neutron production from a source of this type is estimated at 2500 neutrons per second per millicrourie so the flux from this source was approximately  $2.9 \times 10^5$  neutrons per second. Rausa (1) states that the safe dose maximum permissible exposure to polonium-beryllium neutrons for a 30 hour week





is 10 neutrons per square cm. per second. Consequently, the tolerance distance in air for the source was here was about 10 inches.

Willis and others (9) investigated the energy spectrum from a polonium-beryllium neutron source and found that the maximum neutron energy is about 12 Mev. Empirical integration of the spectrum they presented indicated that the neutrons emitted by this type source have an average energy of about 5 Mev.

The gamma ray source used was  $\text{Co}^{60}$ . This source had a strength of approximately  $10 \mu\text{c}$ . Calculations showed that a safe working distance in air for a 1 hour week with this source is slightly less than 2 inches. The  $\text{Co}^{60}$  was contained in a piece of Scotch tape that was rolled into the form of a right cylinder with dimensions of about  $1/8$  inch diameter and  $3/8$  inch high. This was sealed by adding other Scotch tape to it, thus, the source as used had external dimensions of about  $1/4$  inch diameter and 1 inch height.

#### 4. Shielding

The target holder is shown and used as shown in Figure 4. The shield-in box was constructed of lead and was 23 inches by 23 inches by 2 1/2 inches high and the inside diameter of the box was 18 inches by 18 inches by 2 1/2 inches high. The walls of the box were made by sandwiching a 1 1/2 inches thickness of paraffin between two 1/2 inch thicknesses of plywood. The front of the box was removable for access to the counting chamber. The interior was lined with 0.125 inch charcoal sheet. This thickness of charcoal will absorb approximately 90 per cent of the





Figure 4. Apparatus and experimental set-up

A -- Scaler

B -- Voltage regulator

C -- Detector and source suspension rig

D -- Detector and source in position

E -- Stand for holding cylindrical shells

F -- Cylindrical shells

G -- Shielding box with front removed



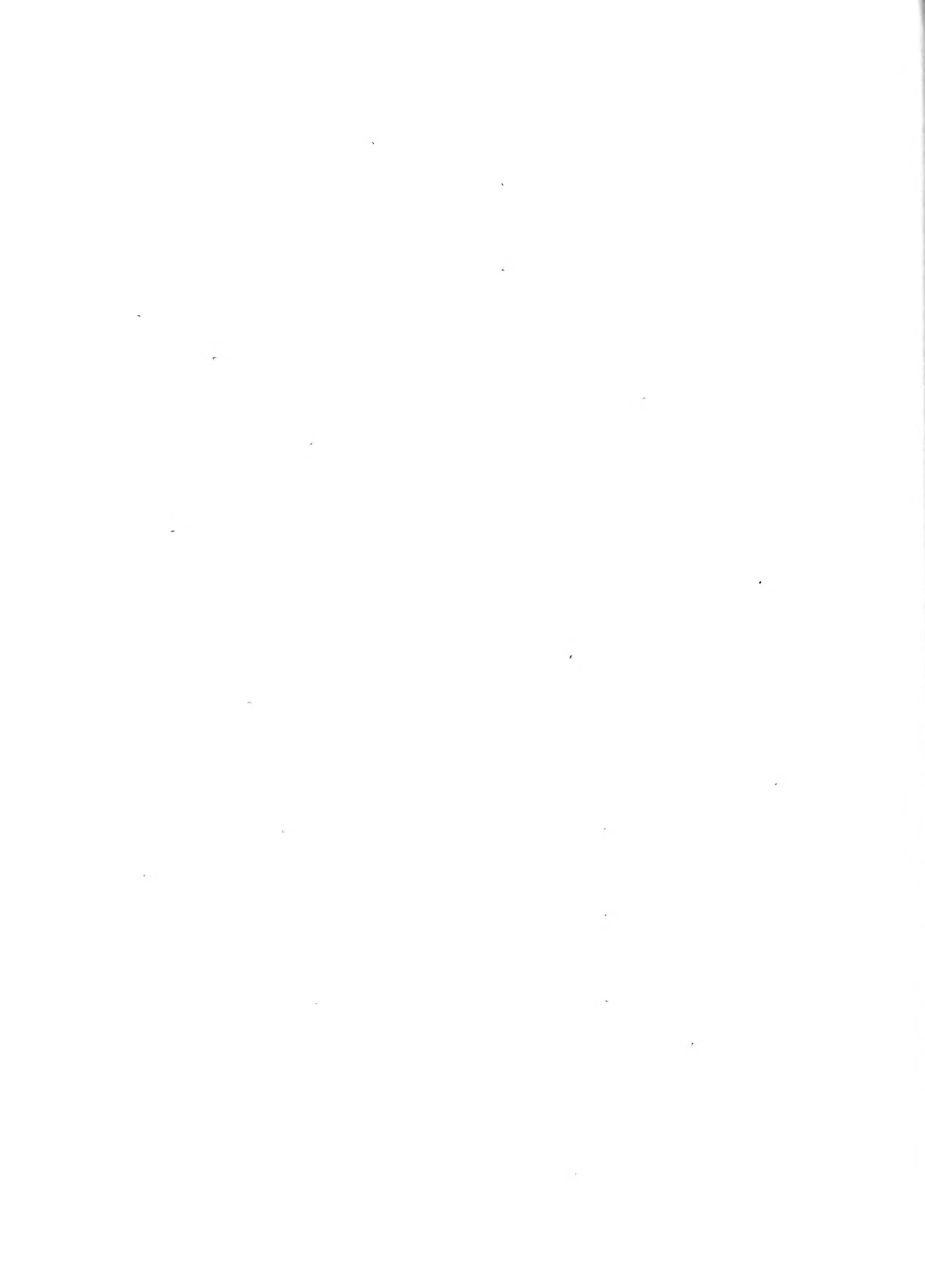


incident neutrons that have energies of 0.25 ev or less which were here defined as slow neutrons. The paraffin-plywood sandwich by moderating any incoming fast neutrons increases the probability of capturing them in the cadmium. A hole to accommodate the counting tube cable was drilled through the center of the top of the box. Two small eye-hooks were screwed into the top of the chamber. The fine cord (approximately 0.015 inch in diameter) that was used for suspending the detector and source was fastened to these hooks.

The 2487 and Alclad 2487 aluminum alloy was rolled into cylindrical shells by the Iowa State College Instrument Shop. Since smooth shells were desired, the longitudinal junction was not riveted or welded but simply held together with Scotch tape, except for two of the heavier gauge shells. For these, due to excessive outward spring action, fine cord had to be used to hold the junction.

All of the seven different cylindrical shells used were 16 inches high. Three of these, rolled from 2487 aluminum alloy sheet, had a shell thickness of 0.025 inch and a radius of 3, 4.5, and 6 inches respectively; two, rolled from Alclad 2487 aluminum alloy sheet, had a shell thickness of 0.064 inch and a radius of 6 and 8 inches respectively; and two, also rolled from Alclad 2487 aluminum alloy sheet, had a shell thickness of 0.126 inch and a radius of 4.5 and 8 inches respectively.

For neutron counting, the counting circuit was composed of a  $3^{10}$  lined proportional counter connected directly to the amplifying circuit of an electronic scaler. The proportional counter was manufactured by





General Electric and has a cylindrical active volume of 1.25 inches in diameter by 3.6 inches in length.

A Model 230 scaler manufactured by the Radiation Instrument Development Laboratory was used. This model has a built-in amplifying circuit and is equipped with a discriminator, a gain control, a register, and a timer. The input voltage to the scaler was maintained at 115 volts by a "Stabilizer" type 135101 voltage regulator.

The operating characteristics of the neutron counting circuit were investigated thoroughly. With the discriminator set at 70 and the gain switch on F, a 25 volt plateau of 2.5 per cent slope was found in the voltage range centered about 675 volts. Thus the operating voltage, discriminator, and gain were set at these values for neutron counting.

A LucasLaird 403 Geiger tube and the above scaler were used to count gamma rays. This Geiger tube has a cylindrical active volume of 1.5 inches diameter and 2.375 inches length.

Additional equipment included a level, a plumb line, and scales.

### C. Procedure

The procedures finally used for counting neutrons and gamma rays were the result of experimenting with various shielding arrangements until the most satisfactory arrangements that were possible with the equipment available were determined.

The shielding box, which was explicitly built for the neutron counting, did not prove satisfactory. It reduced the neutron background, both fast and slow, to practically zero, but did not shield the source and



detector in the box, its scattering of source neutrons greatly overshadowed its value as a shield against fast and slow neutrons impinging on the outside of the box. With the source suspended 4 inches below the detector, the fast neutron count in the box was approximately 20 times the count outside the box and the slow neutron count was approximately tripled. Therefore, the neutron counting was done outside the box.

A few exploratory counts outside the box showed that the scattering from the air and the room was lower with the source suspended some distance above the floor rather than directly next to the floor. Thus, the experimental arrangement shown in Figure 4 resulted.

The shielding box, as expected, was found to be ineffective as a gamma ray shield. The shielding material available included 10 pieces of lead each with dimensions of about  $\frac{1}{2}$  inch by 6 inches by 16 inches, 23 pieces of lead each with dimensions of about  $\frac{3}{4}$  inch by 1 and  $\frac{3}{4}$  inches by 4 inches, and 2 boxes and 2 bags of borated sand averaging about 10 inches in thickness.

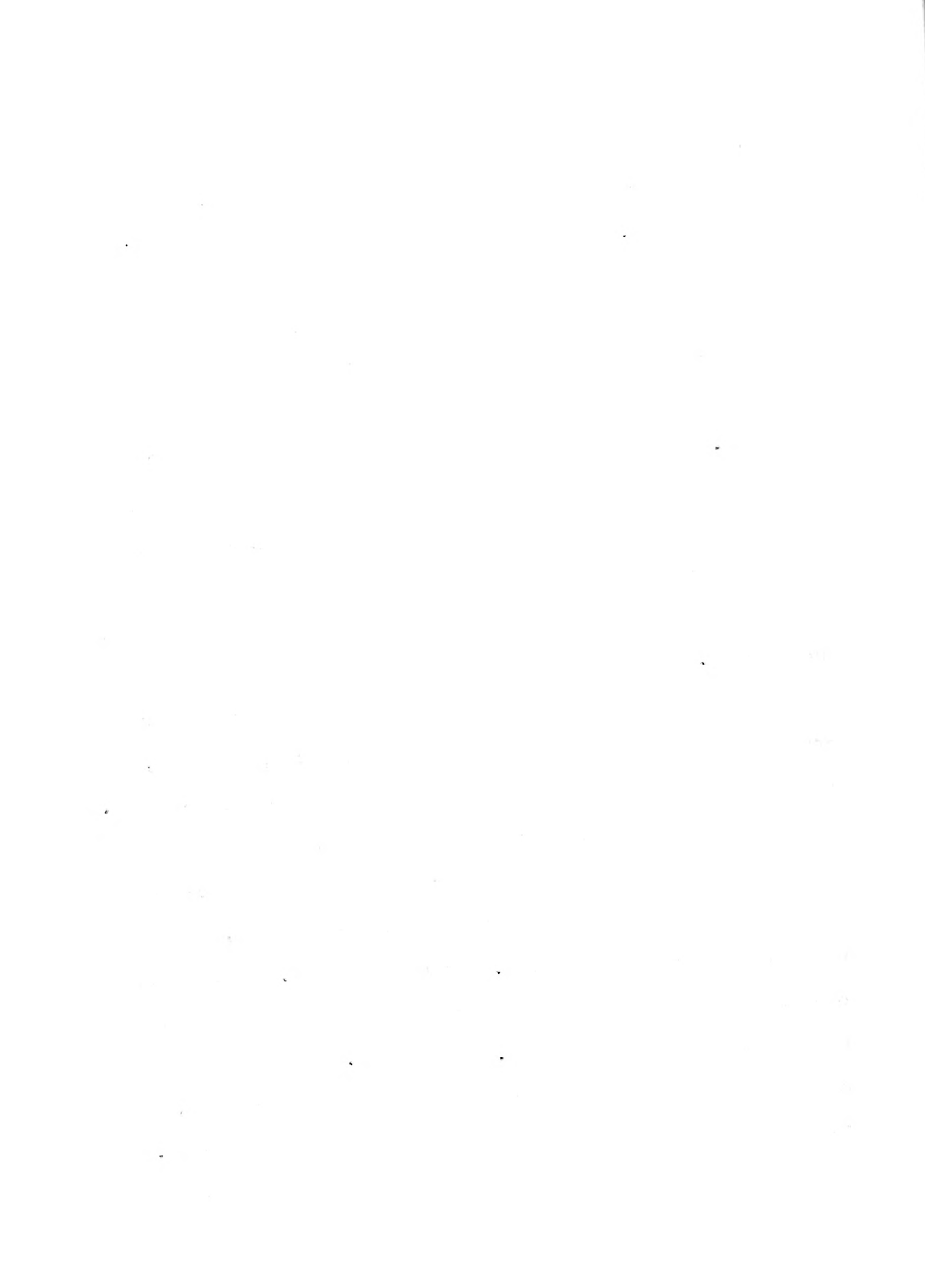
With the gamma ray source and detector suspended in the box, two of the larger pieces of lead were placed on the floor of the counting chamber to determine the effectiveness of the lead in reducing the gamma ray scattering caused by the air and the room. This arrangement did not noticeably reduce the scattering. In fact, with these two pieces of lead in position and all the remaining available lead and the borated sand placed next to the outside of the box, the count still was not noticeably reduced. Therefore, the gamma ray counting was done outside



the box, where a few exploratory counts showed that the scattering from the air and room could be materially reduced over similar scattering inside the box. These exploratory counts indicated that the distance the source and detector was placed above the floor of the room did not influence the scattering appreciably, and that the scattering was reduced to the minimum possible by suspending the source and detector just above the floor with all the available lead placed below them. The best arrangement was found to be  $1\frac{1}{2}$  inches by 16 inches by 16 inches of lead centered directly under the counter and source with the remaining four large pieces of lead placed flat on the floor one on each of the four sides of this central arrangement and with the 23 smaller pieces of lead placed in the spaces between these outer blocks.

The method of suspending the source and detector for gamma ray counting was similar to that shown in figure 4 except, of course, the source and detector were suspended in a position closer to the floor.

All the neutron counts, with the exception of one background count and one other count made to determine the number of slow neutrons being scattered by the air and the room into the detector, were taken with the detector covered with 0.010 inch of cadmium. This thickness of cadmium will capture approximately 90 per cent of the incident neutrons that have energies of 0.25 ev or less. Since any neutron with an energy higher than this was considered to be a fast neutron, the counts taken with the detector covered were due to fast neutrons. Only fast neutron counts were taken because practically all the neutrons



emitted by a source of this type are fast neutrons.

Since the results of this investigation depended to a great extent on the correctness and duplication of geometrical arrangements, every effort was made to assure such conditions for both the neutron and gamma ray measurements. The procedure in each case was identical.

The counting tube was suspended by four pieces of fine cord (approximately 0.016 inch in diameter) which were fastened to four eye-hooks screwed into the upper side of the cross bar of the suspension apparatus. The cords were secured in a manner that would allow the distance between the detector and the cross bar to be either shortened or lengthened by simply turning the hooks in the proper direction. This method was also used to vertically align the counting tube. The distance  $h_1$  between the top of the active volume of the counting tube and the lead blocks in the case of gamma ray counting, or the stand for holding the cylindrical shells in the case of neutron counting was carefully measured with a measuring stick. The vertical alignment of the counting tube was checked with a level and also by sighting along a plumb line that was suspended behind the apparatus. The background counts were made with the counting tubes suspended in this position.

The source was suspended below the detector by a piece of fine cord which was fastened at each end to another piece of cord that was placed around the detector just above its bottom edge. The distance  $h_2$  between the source and the bottom of the active volume of the detector was measured and then checked by measuring the distance from the source to the lead blocks in the case of gamma ray counting, or the

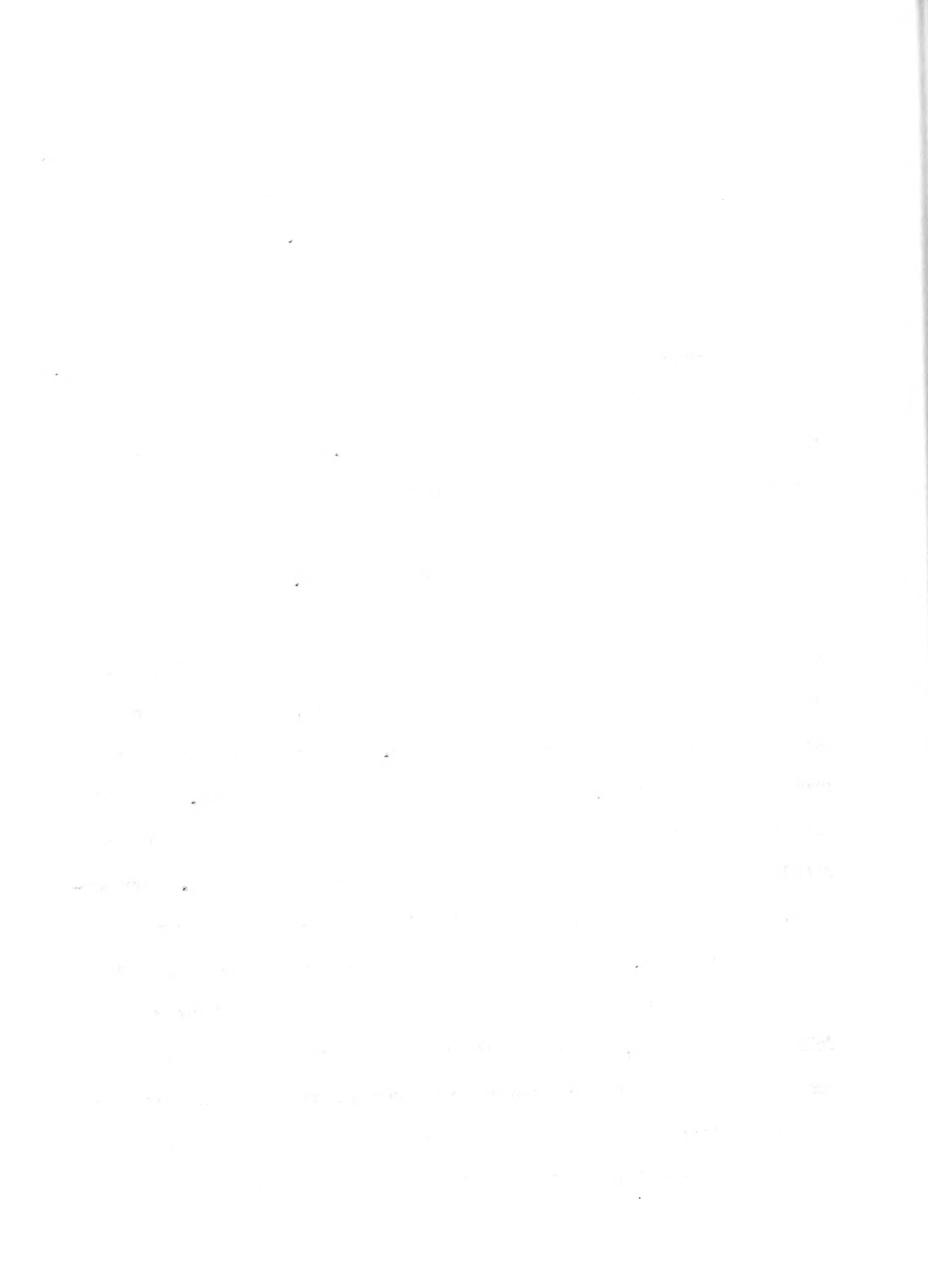




stand for holding the cylindrical shells in the case of neutron counting. These distances were measured from the vertical mid-point of the source as estimated from the dimensions given previously. The centering of the source below the detector was checked by placing the level vertically along the detector so that it projected past the position of the source and then measuring the horizontal distance from the level to the source.

A gamma ray count and both a fast and slow neutron count were made with just the source and detector in position. These counts were made for each value of  $h_s$  used and, when corrected for the scattering caused by the air and room, they are the counts due to the radiation that proceeds directly from the source to the detector.

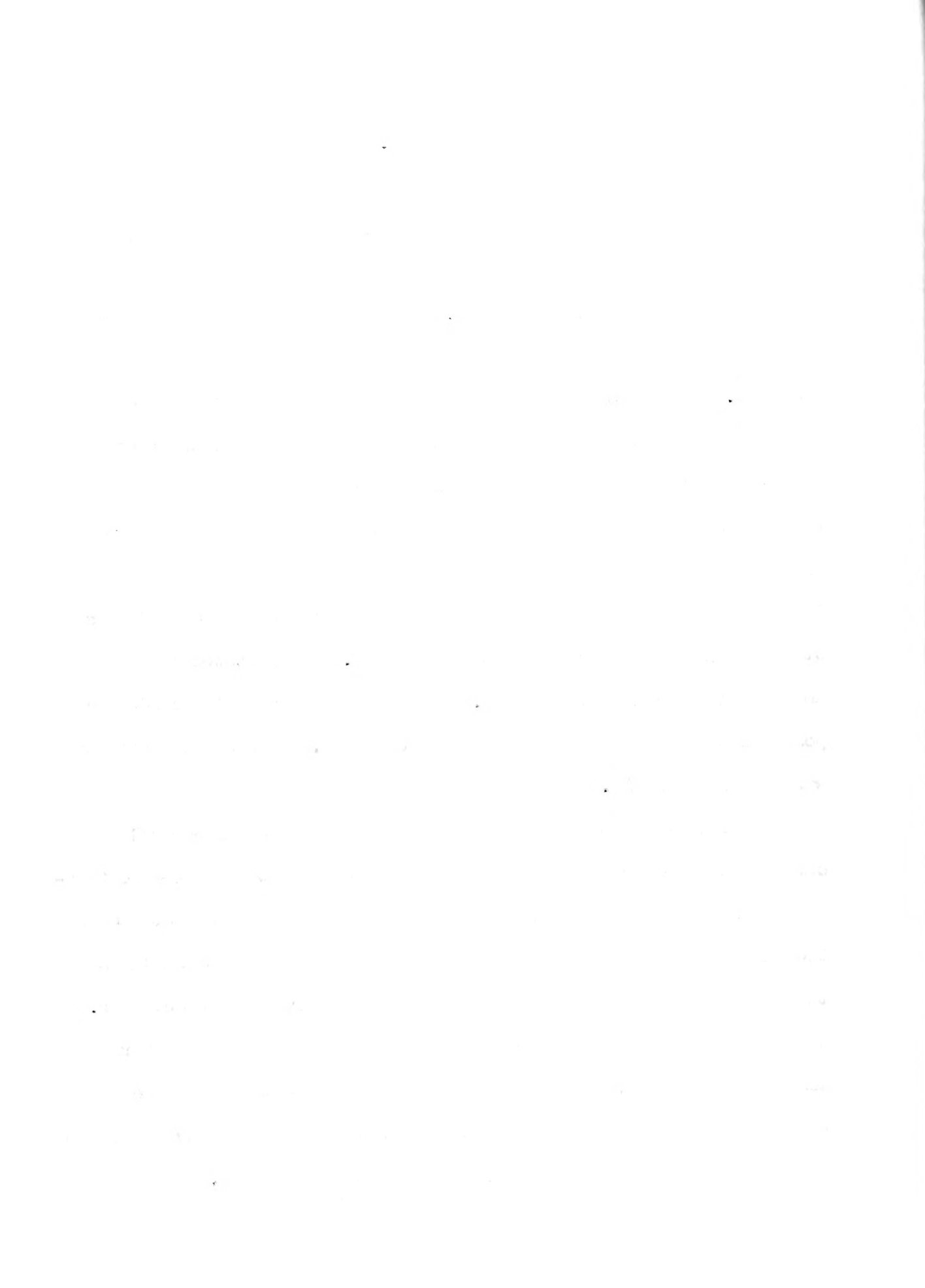
To determine the counts that are caused by the sum of the radiation that proceeds directly and that that is scattered into the detector by the aluminum alloy cylindrical shells, the shells were positioned around the source and detector. The center line of these shells had to coincide with the center line of the detector. This alignment was checked by measuring the distance from the detector wall to the shell at various positions around the periphery of the shell. Furthermore, the shells were checked with the level to determine their vertical alignment. When the neutron detector was covered with cadmium this method of measuring around the periphery of the shell could not be followed, therefore, the seven different cylindrical shells used were positioned with the neutron detector uncovered, suitable markings were made on a piece of heavy paper that was taped to the stand that supported the shells, and these markings were then used for positioning



the shells when the detector was covered.

This system of positioning introduced the possibility of undetected horizontal movement of the alignment paper, the stand, or the detector, or the possibility of the detector and source not remaining aligned with the true vertical. An attempt was made to eliminate these possibilities by making the apparatus concerned as secure as possible. Furthermore, to be sure that the geometry remained the same during the counts, the vertical alignment of the  $B^{10}$  tube was checked before it was covered and again after it was uncovered and after the counts were taken the markings on the piece of paper on the stand were checked by placing one of the cylindrical shells in the position indicated by the markings and measuring to determine if the shell was still centered about the detector and source. In all cases no horizontal movement was detected. Of course this did not exclude the possibility of compensating movements occurring, but such combinations were highly unlikely.

The counts determined by positioning each of the cylindrical shells about the source and the detector were corrected for the scattering caused by the air and room and the resulting count was that due to the sum of the radiation scattered into the detector by the shell and the radiation that proceeds directly from the source to the detector. No correction was made for the secondary effect of the room or air scattered radiation, which normally returned to the counting tube when the cylindrical shell was not in position, being scattered away from the detector by the cylindrical shell when it was in position.



# TABLE 1

## 1. Neutron Scattering

The experimental results for neutron scattering by the aluminum alloy cylindrical shells are listed in Table 1. The difference between the first two counting rates listed for both  $h_5$  equal 4 inches and  $h_5$  equal 3 inches is the counting rate due to slow neutrons. For 3 inches this difference is  $27.3 \pm 1.2$  and for 4 inches it is  $25.7 \pm 1.1$ . Thus, the slow neutron counting rate remained practically constant with these two source positions, indicating that all the slow neutrons reaching the detector were the result of scattering by the air and room and that none of the slow neutrons are issued directly by the source.

The fast neutron counts given in Table 1 had to be corrected for the scattering due to the air and room. In making this correction it was assumed that the number of fast neutrons scattered by the air and room into the counting tube was not influenced by the aluminum cylindrical shells being present or by a small movement of the source.

The magnitude of this correction can be calculated from the formula

$$R_{\text{total}} = R_{\text{source}} + R_{\text{scatter}}$$



Table 1  
Neutron counts

Cylindrical shell dimensions			$h_2$ (in.)	Counting time (minutes)	Net counting rate (R) (counts per minute)	Neutrons counted
r (in.)	t (in.)	$h_1$ (in.)				
3	none	16	3	40	$13.9 \pm 1.1$	fast and slow
	none		3	60	$16.5 \pm 0.5$	fast
	0.025		3	60	$16.1 \pm 0.5$	fast
	0.025		3	60	$16.4 \pm 0.5$	fast
	0.025		3	60	$16.3 \pm 0.5$	fast
4.5	0.064	16	3	60	$17.2 \pm 0.5$	fast
	0.064		3	60	$17.1 \pm 0.5$	fast
	0.126		3	60	$17.4 \pm 0.6$	fast
	0.126		3	60	$16.8 \pm 0.5$	fast
	0.126		3	60	$16.8 \pm 0.5$	fast
6	none	16	4	40	$35.4 \pm 1.0$	fast and slow
	none		4	60	$9.7 \pm 0.4$	fast
	0.025		4	60	$10.1 \pm 0.4$	fast
	0.025		4	60	$10.3 \pm 0.4$	fast
	0.025		4	60	$9.5 \pm 0.4$	fast
8	0.064	16	4	60	$9.9 \pm 0.4$	fast
	0.064		4	60	$9.9 \pm 0.4$	fast
	0.126		4	60	$11.7 \pm 0.4$	fast
	0.126		4	60	$10.2 \pm 0.4$	fast
	0.126		4	60	$10.2 \pm 0.4$	fast

where  $R_{\text{total}}$  is the total fast neutron counting rate

$R_{\text{LF}}$  is the fast neutron counting rate due to those neutrons that proceed directly from the source to the detector

$R_{\text{IF}}$  is the fast neutron counting rate due to those neutrons that are scattered by the air and the room walls to the detector.

100



As the distance  $h_j$  between the source and detector is changed,  $R_{DT}$  will vary according to Equation (16). This equation is based on the assumption of a point source. Calculations made by replacing the neutron source used here with a series of centrally located point sources showed that this assumption is still valid for values of  $h_j$  equal to 3 inches and 4 inches.

The ratio of  $R_{DT}$  at  $h_j$  equal 3 inches to  $R_{DT}$  at  $h_j$  equal 4 inches is then

$$\frac{\left(R_{DT}\right)_3}{\left(R_{DT}\right)_4} = \frac{1 - \cos \beta_{d3}}{1 - \cos \beta_{d4}}$$

where  $\cos \beta_d$  is calculated from the radius of the detector and the distance  $h_j$ . The radius of the detector used here is 0.625 inch, so that the above ratio is 1.75.

Now

$$\left(R_{DT}\right)_3 = \left(R_{DT}\right)_4 - R_{DT}$$

and

$$\left(R_{DT}\right)_4 = \left(R_{DT}\right)_3 - R_{DT}$$

Dividing the first of these equations by the latter, and substituting for the ratio  $\left(R_{DT}\right)_3 / \left(R_{DT}\right)_4$ , and rearranging, results in the equation

$$\frac{2}{9} = \frac{1}{3} = \left( \frac{1}{3} \right)^2$$

8.2.1

$$- \left( \frac{1}{3} \right) = \left( \frac{1}{3} \right)$$

$$- \left( \frac{1}{3} \right) = \left( \frac{1}{3} \right)$$

$$- \left( \frac{1}{3} \right) \left( \frac{1}{3} \right)$$

Table 2

Fast neutron counting rates corrected for air and room scattering and total neutron scattering ratios

Cylindrical shell dimensions		$h_5$ (in.)	Net counting rate (counts per minute)		$R_T$ experimental	$R_T$ theoretical
r (in.)	t (in.)		$R - R_{WF}$ (counts per minute)	$R_{WF}$ (counts per minute)		
none		3	$16.3 \pm 0.5$	$15.1 \pm 1.3$		
3	0.025	3	$16.1 \pm 0.5$	$15.4 \pm 1.3$	$0.975 \pm 0.115$	1.020
4.5	0.025	3	$16.4 \pm 0.5$	$15.7 \pm 1.3$	$0.995 \pm 0.116$	1.013
6	0.025	3	$16.3 \pm 0.5$	$16.1 \pm 1.3$	$1.020 \pm 0.116$	1.003
6	0.064	3	$17.2 \pm 0.5$	$16.5 \pm 1.3$	$1.044 \pm 0.119$	1.020
8	0.064	3	$17.1 \pm 0.5$	$16.4 \pm 1.3$	$1.030 \pm 0.119$	1.010
4.5	0.126	3	$17.4 \pm 0.6$	$16.7 \pm 1.3$	$1.050 \pm 0.120$	1.067
8	0.126	3	$16.7 \pm 0.5$	$16.1 \pm 1.3$	$1.020 \pm 0.116$	1.020
none		4	$9.7 \pm 0.4$	$9.0 \pm 1.3$		
3	0.025	4	$10.1 \pm 0.4$	$9.4 \pm 1.3$	$1.044 \pm 0.209$	1.047
4.5	0.025	4	$10.3 \pm 0.4$	$9.6 \pm 1.3$	$1.067 \pm 0.211$	1.023
6	0.025	4	$9.5 \pm 0.4$	$8.7 \pm 1.3$	$0.967 \pm 0.200$	1.013
6	0.064	4	$9.2 \pm 0.4$	$9.2 \pm 1.3$	$1.022 \pm 0.205$	1.034
8	0.064	4	$9.2 \pm 0.4$	$9.2 \pm 1.3$	$1.022 \pm 0.205$	1.018
4.5	0.126	4	$11.7 \pm 0.4$	$11.0 \pm 1.3$	$1.112 \pm 0.230$	1.115
8	0.126	4	$10.2 \pm 0.4$	$9.4 \pm 1.3$	$1.044 \pm 0.209$	1.035

$$R_{WF} = \frac{1.75 \left( \frac{R}{r} \right)_4 - \left( \frac{R}{r} \right)_3}{0.75}$$

This equation, upon substituting the fast neutron counting rates without a cylindrical shell in position for the two values of  $h_5$  used, gave a value of  $0.7 \pm 1.2$  counts per minute for  $R_{WF}$ . The fast neutron counting rates corrected for this scattering are given in table 2.

The value of  $h_5$  is 16 inches for all the cylindrical shells, therefore,

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100	101	102	103	104	105	106	107	108	109	110	111	112	113	114	115	116	117	118	119	120	121	122	123	124	125	126	127	128	129	130	131	132	133	134	135	136	137	138	139	140	141	142	143	144	145	146	147	148	149	150	151	152	153	154	155	156	157	158	159	160	161	162	163	164	165	166	167	168	169	170	171	172	173	174	175	176	177	178	179	180	181	182	183	184	185	186	187	188	189	190	191	192	193	194	195	196	197	198	199	200	201	202	203	204	205	206	207	208	209	210	211	212	213	214	215	216	217	218	219	220	221	222	223	224	225	226	227	228	229	230	231	232	233	234	235	236	237	238	239	240	241	242	243	244	245	246	247	248	249	250	251	252	253	254	255	256	257	258	259	260	261	262	263	264	265	266	267	268	269	270	271	272	273	274	275	276	277	278	279	280	281	282	283	284	285	286	287	288	289	290	291	292	293	294	295	296	297	298	299	300	301	302	303	304	305	306	307	308	309	310	311	312	313	314	315	316	317	318	319	320	321	322	323	324	325	326	327	328	329	330	331	332	333	334	335	336	337	338	339	340	341	342	343	344	345	346	347	348	349	350	351	352	353	354	355	356	357	358	359	360	361	362	363	364	365	366	367	368	369	370	371	372	373	374	375	376	377	378	379	380	381	382	383	384	385	386	387	388	389	390	391	392	393	394	395	396	397	398	399	400	401	402	403	404	405	406	407	408	409	410	411	412	413	414	415	416	417	418	419	420	421	422	423	424	425	426	427	428	429	430	431	432	433	434	435	436	437	438	439	440	441	442	443	444	445	446	447	448	449	450	451	452	453	454	455	456	457	458	459	460	461	462	463	464	465	466	467	468	469	470	471	472	473	474	475	476	477	478	479	480	481	482	483	484	485	486	487	488	489	490	491	492	493	494	495	496	497	498	499	500	501	502	503	504	505	506	507	508	509	510	511	512	513	514	515	516	517	518	519	520	521	522	523	524	525	526	527	528	529	530	531	532	533	534	535	536	537	538	539	540	541	542	543	544	545	546	547	548	549	550	551	552	553	554	555	556	557	558	559	560	561	562	563	564	565	566	567	568	569	570	571	572	573	574	575	576	577	578	579	580	581	582	583	584	585	586	587	588	589	590	591	592	593	594	595	596	597	598	599	600	601	602	603	604	605	606	607	608	609	610	611	612	613	614	615	616	617	618	619	620	621	622	623	624	625	626	627	628	629	630	631	632	633	634	635	636	637	638	639	640	641	642	643	644	645	646	647	648	649	650	651	652	653	654	655	656	657	658	659	660	661	662	663	664	665	666	667	668	669	670	671	672	673	674	675	676	677	678	679	680	681	682	683	684	685	686	687	688	689	690	691	692	693	694	695	696	697	698	699	700	701	702	703	704	705	706	707	708	709	710	711	712	713	714	715	716	717	718	719	720	721	722	723	724	725	726	727	728	729	730	731	732	733	734	735	736	737	738	739	740	741	742	743	744	745	746	747	748	749	750	751	752	753	754	755	756	757	758	759	760	761	762	763	764	765	766	767	768	769	770	771	772	773	774	775	776	777	778	779	780	781	782	783	784	785	786	787	788	789	790	791	792	793	794	795	796	797	798	799	800	801	802	803	804	805	806	807	808	809	810	811	812	813	814	815	816	817	818	819	820	821	822	823	824	825	826	827	828	829	830	831	832	833	834	835	836	837	838	839	840	841	842	843	844	845	846	847	848	849	850	851	852	853	854	855	856	857	858	859	860	861	862	863	864	865	866	867	868	869	870	871	872	873	874	875	876	877	878	879	880	881	882	883	884	885	886	887	888	889	890	891	892	893	894	895	896	897	898	899	900	901	902	903	904	905	906	907	908	909	910	911	912	913	914	915	916	917	918	919	920	921	922	923	924	925	926	927	928	929	930	931	932	933	934	935	936	937	938	939	940	941	942	943	944	945	946	947	948	949	950	951	952	953	954	955	956	957	958	959	960	961	962	963	964	965	966	967	968	969	970	971	972	973	974	975	976	977	978	979	980	981	982	983	984	985	986	987	988	989	990	991	992	993	994	995	996	997	998	999	1000	1001	1002	1003	1004	1005	1006	1007	1008	1009	1010	1011	1012	1013	1014	1015	1016	1017	1018	1019	1020	1021	1022	1023	1024	1025	1026	1027	1028	1029	1030	1031	1032	1033	1034	1035	1036	1037	1038	1039	1040	1041	1042	1043	1044	1045	1046	1047	1048	1049	1050	1051	1052	1053	1054	1055	1056	1057	1058	1059	1060	1061	1062	1063	1064	1065	1066	1067	1068	1069	1070	1071	1072	1073	1074	1075	1076	1077	1078	1079	1080	1081	1082	1083	1084	1085	1086	1087	1088	1089	1090	1091	1092	1093	1094	1095	1096	1097	1098	1099	1100	1101	1102	1103	1104	1105	1106	1107	1108	1109	1110	1111	1112	1113	1114	1115	1116	1117	1118	1119	1120	1121	1122	1123	1124	1125	1126	1127	1128	1129	1130	1131	1132	1133	1134	1135	1136	1137	1138	1139	1140	1141	1142	1143	1144	1145	1146	1147	1148	1149	1150	1151	1152	1153	1154	1155	1156	1157	1158	1159	1160	1161	1162	1163	1164	1165	1166	1167	1168	1169	1170	1171	1172	1173	1174	1175	1176	1177	1178	1179	1180	1181	1182	1183	1184	1185	1186	1187	1188	1189	1190	1191	1192	1193	1194	1195	1196	1197	1198	1199	1200	1201	1202	1203	1204	1205	1206	1207	1208	1209	1210	1211	1212	1213	1214	1215	1216	1217	1218	1219	1220	1221	1222	1223	1224	1225	1226	1227	1228	1229	1230	1231	1232	1233	1234	1235	1236	1237	1238	1239	1240	1241	1242	1243	1244	1245	1246	1247	1248	1249	1250	1251	1252	1253	1254	1255	1256	1257	1258	1259	1260	1261	1262	1263	1264	1265	1266	1267	1268	1269	1270	1271	1272	1273	1274	1275	1276	1277	1278	1279	1280	1281	1282	1283	1284	1285	1286	1287	1288	1289	1290	1291	1292	1293	1294	1295	1296	1297	1298	1299	1300	1301	1302	1303	1304	1305	1306	1307	1308	1309	1310	1311	1312	1313	1314	1315	1316	1317	1318	1319	1320	1321	1322	1323	1324	1325	1326	1327	1328	1329	1330	1331	1332	1333	1334	1335	1336	1337	1338	1339	1340	1341	1342	1343	1344	1345	1346	1347	1348	1349	1350	1351	1352	1353	1354	1355	1356	1357	1358	1359	1360	1361	1362	1363	1364	1365	1366	1367	1368	1369	1370	1371	1372	1373	1374	1375	1376	1377	1378	1379	1380	1381	1382	1383	1384	1385	1386	1387	1388	1389	1390	1391	1392	1393	1394	1395	1396	1397	1398	1399	1400	1401	1402	1403	1404	1405	1406	1407	1408	1409	1410	1411	1412	1413	1414	1415	1416	1417	1418	1419	1420	1421	1422	1423	1424	1425	1426	1427	1428	1429	1430	1431	1432	1433	1434	1435	1436	1437	1438	1439	1440	1441	1442	1443	1444	1445	1446	1447	1448	1449	1450	1451	1452	1453	1454	1455	1456	1457	1458	1459	1460	1461	1462	1463	1464	1465	1466	1467	1468	1469	1470	1471	1472	1473	1474	1475	1476	1477	1478	1479	1480	1481	1482	1483	1484	1485	1486	1487	1488	1489	1490	1491	1492	1493	1494	1495	1
---	---	---	---	---	---	---	---	---	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	---

it is not listed in this table.

The experimental total neutron scattering ratios  $R_T$ , as determined by dividing each corrected counting rate taken with a cylindrical shell in position by the corrected counting rate when no shell was in position, is also listed. The last column in Table 2 lists the theoretical values of  $R_T$  which were computed by using Equation (15).

Any comparison of the experimental results with the theoretical values of  $R_T$  was impossible due to the statistical deviations in the experimental values. This large statistical deviation is for the most part caused by the deviation in the counting rate due to the scattering from the air and the room. Every possible effort was made to reduce this unwanted scattering to a statistically acceptable level, however, these efforts were not successful.

### B. Gamma Ray Scattering

The experimental results for gamma ray scattering by the aluminum alloy cylindrical shells are listed in Table 3. Since  $h_p$  is 16 inches for all the shells it is not listed in the table.

The net counting rates listed in the last column of Table 3 had to be corrected for the scattering due to the air and room. This correction was made in a manner identical to that used for the correction to the neutron counting rates. The gamma ray source was much smaller in dimensions than the neutron source, thus the assumption of a point source, as is required to apply Equation (1') is valid.

1. The first part of the document is a list of names and addresses of the members of the committee.

Name		Address	
Mr. A. B. C.	123	456	789
Mr. D. E. F.	101	202	303
Mr. G. H. I.	404	505	606
Mr. J. K. L.	707	808	909
Mr. M. N. O.	111	222	333
Mr. P. Q. R.	444	555	666
Mr. S. T. U.	777	888	999
Mr. V. W. X.	1010	1111	1212
Mr. Y. Z. A.	1313	1414	1515
Mr. B. C. D.	1616	1717	1818
Mr. E. F. G.	1919	2020	2121
Mr. H. I. J.	2222	2323	2424
Mr. K. L. M.	2525	2626	2727
Mr. N. O. P.	2828	2929	3030
Mr. Q. R. S.	3131	3232	3333
Mr. T. U. V.	3434	3535	3636
Mr. W. X. Y.	3737	3838	3939
Mr. Z. A. B.	4040	4141	4242
Mr. C. D. E.	4343	4444	4545
Mr. F. G. H.	4646	4747	4848
Mr. I. J. K.	4949	5050	5151
Mr. L. M. N.	5252	5353	5454
Mr. O. P. Q.	5555	5656	5757
Mr. R. S. T.	5858	5959	6060
Mr. U. V. W.	6161	6262	6363
Mr. X. Y. Z.	6464	6565	6666
Mr. A. B. C.	6767	6868	6969
Mr. D. E. F.	7070	7171	7272
Mr. G. H. I.	7373	7474	7575
Mr. J. K. L.	7676	7777	7878
Mr. M. N. O.	7979	8080	8181
Mr. P. Q. R.	8282	8383	8484
Mr. S. T. U.	8585	8686	8787
Mr. V. W. X.	8888	8989	9090
Mr. Y. Z. A.	9191	9292	9393
Mr. B. C. D.	9494	9595	9696
Mr. E. F. G.	9797	9898	9999

2. The second part of the document is a list of names and addresses of the members of the committee.

3. The third part of the document is a list of names and addresses of the members of the committee.

Table 4

gross  $\gamma$  counting rates corrected for air and room scattering and total gross  $\gamma$  scattering ratios

Cylindrical shell dimensions		$h_T$ (in.)	Net counting rate ( ) (counts per minute)	$S - R_{T,\gamma}$ (counts per minute)	$R_{T,\gamma}$ experimental	$R_{T,\gamma}$ theoretical
r (in.)	t (in.)					
none		4	4792 $\pm$ 31	3973 $\pm$ 51		
3	0.025	4	4823 $\pm$ 32	4041 $\pm$ 52	1.015 $\pm$ 0.017	1.010
4.5	0.025	4	4852 $\pm$ 32	4071 $\pm$ 52	1.025 $\pm$ 0.019	1.005
6	0.025	4	4790 $\pm$ 32	4016 $\pm$ 52	1.012 $\pm$ 0.015	1.007
4.5	0.126	4	4875 $\pm$ 32	4095 $\pm$ 52	1.031 $\pm$ 0.019	1.024
2	0.126	4	4852 $\pm$ 32	4069 $\pm$ 52	1.025 $\pm$ 0.019	1.007
none		6	2587 $\pm$ 17	1905 $\pm$ 14		
3	0.025	6	2635 $\pm$ 17	1933 $\pm$ 14	1.055 $\pm$ 0.034	1.023
4.5	0.025	6	2605 $\pm$ 17	1923 $\pm$ 14	1.010 $\pm$ 0.035	1.019
6	0.025	6	2610 $\pm$ 17	1924 $\pm$ 14	1.013 $\pm$ 0.035	1.006
6	0.064	6	2650 $\pm$ 17	1964 $\pm$ 14	1.035 $\pm$ 0.035	1.015
8	0.064	6	2597 $\pm$ 17	1919 $\pm$ 14	1.006 $\pm$ 0.035	1.008
4.5	0.126	6	2731 $\pm$ 17	1947 $\pm$ 14	1.080 $\pm$ 0.036	1.052
8	0.126	6	2643 $\pm$ 17	1941 $\pm$ 14	1.031 $\pm$ 0.035	1.016

It was observed that the value of  $R_{T,\gamma}$  remains constant with or without the electric 2 shell, positioned around the source and detector. The gross  $\gamma$  counting rates corrected for  $R_{T,\gamma}$  are listed in Table 4. The experimentally determined total gross  $\gamma$  scattering ratios are also listed. These ratios were calculated by dividing the corrected gross  $\gamma$  counting rate of the electric 2 shell in position by the counts of counting rate when the shell was in position. The theoretical values of  $R_{T,\gamma}$ , calculated from equation (24), are listed in the last

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100	101	102	103	104	105	106	107	108	109	110	111	112	113	114	115	116	117	118	119	120	121	122	123	124	125	126	127	128	129	130	131	132	133	134	135	136	137	138	139	140	141	142	143	144	145	146	147	148	149	150	151	152	153	154	155	156	157	158	159	160	161	162	163	164	165	166	167	168	169	170	171	172	173	174	175	176	177	178	179	180	181	182	183	184	185	186	187	188	189	190	191	192	193	194	195	196	197	198	199	200	201	202	203	204	205	206	207	208	209	210	211	212	213	214	215	216	217	218	219	220	221	222	223	224	225	226	227	228	229	230	231	232	233	234	235	236	237	238	239	240	241	242	243	244	245	246	247	248	249	250	251	252	253	254	255	256	257	258	259	260	261	262	263	264	265	266	267	268	269	270	271	272	273	274	275	276	277	278	279	280	281	282	283	284	285	286	287	288	289	290	291	292	293	294	295	296	297	298	299	300	301	302	303	304	305	306	307	308	309	310	311	312	313	314	315	316	317	318	319	320	321	322	323	324	325	326	327	328	329	330	331	332	333	334	335	336	337	338	339	340	341	342	343	344	345	346	347	348	349	350	351	352	353	354	355	356	357	358	359	360	361	362	363	364	365	366	367	368	369	370	371	372	373	374	375	376	377	378	379	380	381	382	383	384	385	386	387	388	389	390	391	392	393	394	395	396	397	398	399	400	401	402	403	404	405	406	407	408	409	410	411	412	413	414	415	416	417	418	419	420	421	422	423	424	425	426	427	428	429	430	431	432	433	434	435	436	437	438	439	440	441	442	443	444	445	446	447	448	449	450	451	452	453	454	455	456	457	458	459	460	461	462	463	464	465	466	467	468	469	470	471	472	473	474	475	476	477	478	479	480	481	482	483	484	485	486	487	488	489	490	491	492	493	494	495	496	497	498	499	500	501	502	503	504	505	506	507	508	509	510	511	512	513	514	515	516	517	518	519	520	521	522	523	524	525	526	527	528	529	530	531	532	533	534	535	536	537	538	539	540	541	542	543	544	545	546	547	548	549	550	551	552	553	554	555	556	557	558	559	560	561	562	563	564	565	566	567	568	569	570	571	572	573	574	575	576	577	578	579	580	581	582	583	584	585	586	587	588	589	590	591	592	593	594	595	596	597	598	599	600	601	602	603	604	605	606	607	608	609	610	611	612	613	614	615	616	617	618	619	620	621	622	623	624	625	626	627	628	629	630	631	632	633	634	635	636	637	638	639	640	641	642	643	644	645	646	647	648	649	650	651	652	653	654	655	656	657	658	659	660	661	662	663	664	665	666	667	668	669	670	671	672	673	674	675	676	677	678	679	680	681	682	683	684	685	686	687	688	689	690	691	692	693	694	695	696	697	698	699	700	701	702	703	704	705	706	707	708	709	710	711	712	713	714	715	716	717	718	719	720	721	722	723	724	725	726	727	728	729	730	731	732	733	734	735	736	737	738	739	740	741	742	743	744	745	746	747	748	749	750	751	752	753	754	755	756	757	758	759	760	761	762	763	764	765	766	767	768	769	770	771	772	773	774	775	776	777	778	779	780	781	782	783	784	785	786	787	788	789	790	791	792	793	794	795	796	797	798	799	800	801	802	803	804	805	806	807	808	809	810	811	812	813	814	815	816	817	818	819	820	821	822	823	824	825	826	827	828	829	830	831	832	833	834	835	836	837	838	839	840	841	842	843	844	845	846	847	848	849	850	851	852	853	854	855	856	857	858	859	860	861	862	863	864	865	866	867	868	869	870	871	872	873	874	875	876	877	878	879	880	881	882	883	884	885	886	887	888	889	890	891	892	893	894	895	896	897	898	899	900	901	902	903	904	905	906	907	908	909	910	911	912	913	914	915	916	917	918	919	920	921	922	923	924	925	926	927	928	929	930	931	932	933	934	935	936	937	938	939	940	941	942	943	944	945	946	947	948	949	950	951	952	953	954	955	956	957	958	959	960	961	962	963	964	965	966	967	968	969	970	971	972	973	974	975	976	977	978	979	980	981	982	983	984	985	986	987	988	989	990	991	992	993	994	995	996	997	998	999	1000	1001	1002	1003	1004	1005	1006	1007	1008	1009	1010	1011	1012	1013	1014	1015	1016	1017	1018	1019	1020	1021	1022	1023	1024	1025	1026	1027	1028	1029	1030	1031	1032	1033	1034	1035	1036	1037	1038	1039	1040	1041	1042	1043	1044	1045	1046	1047	1048	1049	1050	1051	1052	1053	1054	1055	1056	1057	1058	1059	1060	1061	1062	1063	1064	1065	1066	1067	1068	1069	1070	1071	1072	1073	1074	1075	1076	1077	1078	1079	1080	1081	1082	1083	1084	1085	1086	1087	1088	1089	1090	1091	1092	1093	1094	1095	1096	1097	1098	1099	1100	1101	1102	1103	1104	1105	1106	1107	1108	1109	1110	1111	1112	1113	1114	1115	1116	1117	1118	1119	1120	1121	1122	1123	1124	1125	1126	1127	1128	1129	1130	1131	1132	1133	1134	1135	1136	1137	1138	1139	1140	1141	1142	1143	1144	1145	1146	1147	1148	1149	1150	1151	1152	1153	1154	1155	1156	1157	1158	1159	1160	1161	1162	1163	1164	1165	1166	1167	1168	1169	1170	1171	1172	1173	1174	1175	1176	1177	1178	1179	1180	1181	1182	1183	1184	1185	1186	1187	1188	1189	1190	1191	1192	1193	1194	1195	1196	1197	1198	1199	1200	1201	1202	1203	1204	1205	1206	1207	1208	1209	1210	1211	1212	1213	1214	1215	1216	1217	1218	1219	1220	1221	1222	1223	1224	1225	1226	1227	1228	1229	1230	1231	1232	1233	1234	1235	1236	1237	1238	1239	1240	1241	1242	1243	1244	1245	1246	1247	1248	1249	1250	1251	1252	1253	1254	1255	1256	1257	1258	1259	1260	1261	1262	1263	1264	1265	1266	1267	1268	1269	1270	1271	1272	1273	1274	1275	1276	1277	1278	1279	1280	1281	1282	1283	1284	1285	1286	1287	1288	1289	1290	1291	1292	1293	1294	1295	1296	1297	1298	1299	1300	1301	1302	1303	1304	1305	1306	1307	1308	1309	1310	1311	1312	1313	1314	1315	1316	1317	1318	1319	1320	1321	1322	1323	1324	1325	1326	1327	1328	1329	1330	1331	1332	1333	1334	1335	1336	1337	1338	1339	1340	1341	1342	1343	1344	1345	1346	1347	1348	1349	1350	1351	1352	1353	1354	1355	1356	1357	1358	1359	1360	1361	1362	1363	1364	1365	1366	1367	1368	1369	1370	1371	1372	1373	1374	1375	1376	1377	1378	1379	1380	1381	1382	1383	1384	1385	1386	1387	1388	1389	1390	1391	1392	1393	1394	1395	1396	1397	1398	1399	1400	1401	1402	1403	1404	1405	1406	1407	1408	1409	1410	1411	1412	1413	1414	1415	1416	1417	1418	1419	1420	1421	1422	1423	1424	1425	1426	1427	1428	1429	1430	1431	1432	1433	1434	1435	1436	1437	1438	1439	1440	1441	1442	1443	1444	1445	1446	1447	1448	1449	1450	1451	1452	1453	1454	1455	1456	1457	1458	1459	1460	1461	1462	1463	1464	1465	1466	1467	1468	1469	1470	1471	1472	1473	1474	1475	1476	1477	1478	1479	1480	1481	1482	1483	1484	1485	1486	1487	1488	1489	1490	1491	1492	1493	1494	1495	1
---	---	---	---	---	---	---	---	---	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	-----	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	------	---



column of table 4.

An examination of the experimental values of  $R_{T\gamma}$  shows that in certain cases, they tend to support the theoretical values. However, the statistical deviations in the experimental values are too broad to make any positive comparison between them and the theoretical values. For instance, with the cylindrical shell of 3 inches radius and 0.025 inch shell thickness and with  $h_0$  equal to 6 inches, the percentage variation between the theoretical and the experimental value as found from the equation,

$$\text{percentage variation} = \frac{(R_{T\gamma})_{\text{experimental}} - (R_{T\gamma})_{\text{theoretical}}}{(R_{T\gamma})_{\text{theoretical}}} \times 100$$

is  $3.12 \pm 3.52$  per cent.

As in the experimental results for neutron scattering, the predominant contribution to the large deviations was the statistical variation in the calculated counting rate due to the air and the room scattering. This was reduced to the lowest possible value with the equipment available, but as is evident it was not reduced enough.

#### C. General Discussion

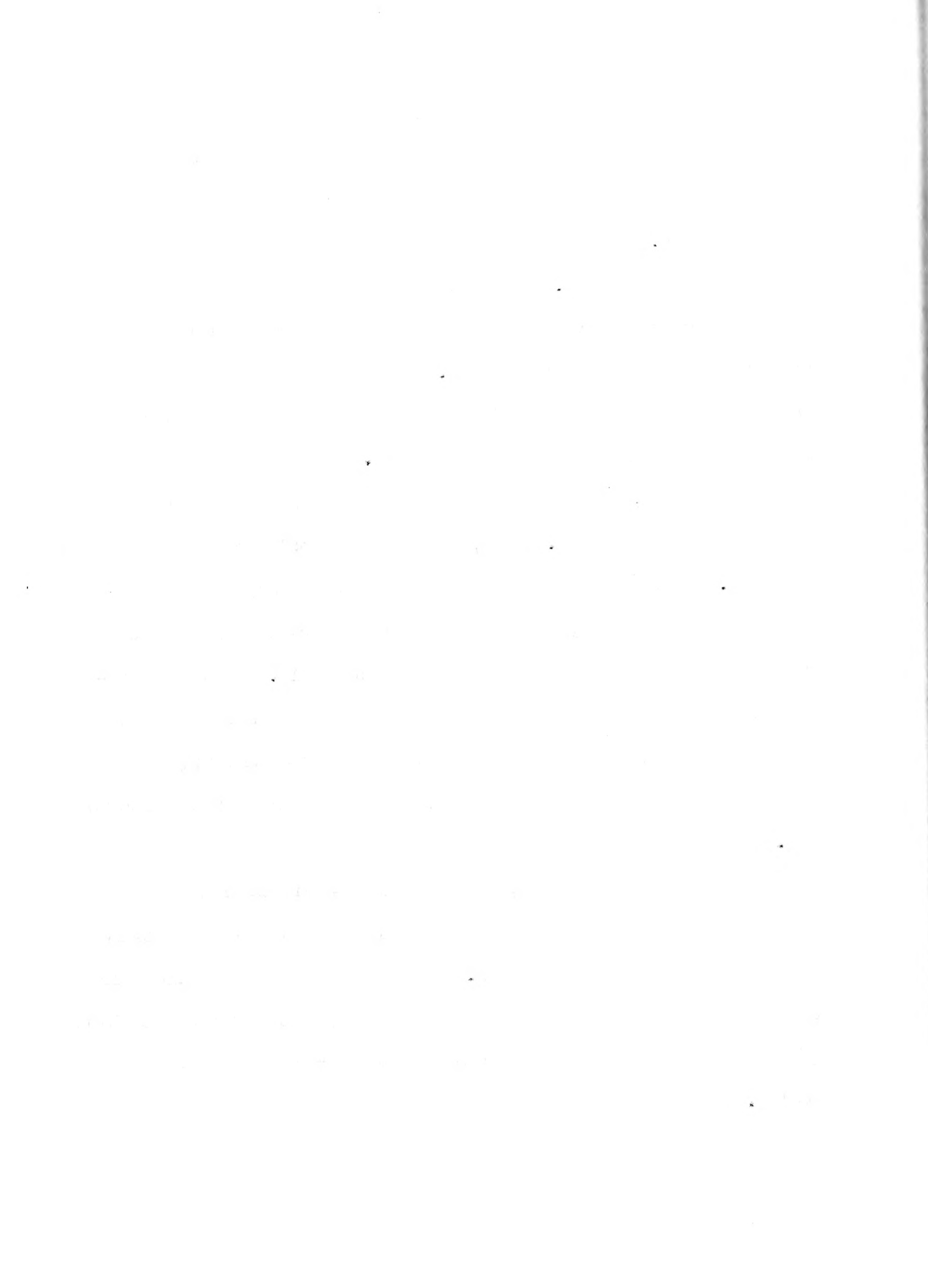
It is believed that an experimental procedure which will give useful results can be devised for general gamma radiation scattering by aluminum alloy cylindrical shells.



In the case of neutron counting, a detector with a higher efficiency for counting fast neutrons or a stronger source or a combination of these two would increase the probability of securing useful results. For gamma ray counting, the taking of longer counts may improve the results. However, it is still a probability that the scattering caused by the air and the room would be the predominating factor in the statistical accuracy. If this is found to be true, another method of experimentally determining the scattering caused by the cylindrical shells would be desirable.

In any room, the scattering caused by the air and the room is mainly due to the latter. Thus, the logical conclusion is to eliminate the room. This can be done by suspending the source, detector, and cylindrical shell from, say, a guide wire of a radio tower or some other similar structure as was done by Glasgow (1). If the experimental system is some distance above the ground and far enough away from the tower or other structure, the system is essentially in an infinite air medium and the only conspicuous scatter would be from the air.

As a further refinement, the equations developed in this investigation for radiation scattering could be modified to include the scattering caused by the air. Glasgow (1) gave an equation for scattering of neutrons in an infinite air medium and Hackett and Cohen (5) presented an equation for gamma ray scattering by an infinite medium.



## VII. CONCLUSIONS

The experimental results, although tending to support the theoretical gamma ray scattering calculations, did not prove or disprove the analytical investigation results.

A more elaborate experimental system and procedure and a more efficient fast neutron detector or a stronger source or both would probably be needed to secure useful experimental results.

The scattering of neutrons and gamma rays by the air and the room was the predominant factor in producing the large statistical deviations in the corrected counting rates. These statistical deviations were the major cause of the poor results, although the low neutron counting rates were a contributing factor.



## VIII. LITERATURE CITED

1. Glasgow, D. W. Neutron scattering from the walls and air of a laboratory. Richland, Washington. Hanford Atomic Products Operation HW-32086. June 9, 1954.
2. Plesset, M. S. Scattering of gamma rays and neutrons. Douglas Aircraft Company, Project Rand Report RAD-196. April 29, 1947. (Original not available for examination; abstracted in Nuclear Science Abstracts. 1: 522. 1948.)
3. Plesset, M. S. and others. Effect of source and shadow shield geometry on the scattering of gamma rays. Douglas Aircraft Company, Project Rand Report RAD-236. February 26, 1948. (Original not available for examination; abstracted in Nuclear Science Abstracts. 1: 430. 1948.)
4. Hine, Gerald J. and McCall, Richard C. Gamma-ray back-scattering. Nucleonics. 12: 27-30. April, 1954.
5. Plesset, M. S. and Cohen, S. F. Scattering and absorption of gamma-rays. Journal of Applied Physics. 22: 350-357. 1951.
6. Alcoa aluminum and its alloys. Pittsburg, Pa., Aluminum Company of America. 1947.
7. Glasstone, Samuel and Heland, Hilton C. The elements of nuclear reactor theory. New York, E. Van Nostrand Company, Inc. 1952.
8. Hause, Gerald J. Gamma dose rate from a Po-Be source. Nucleonics. 12: 62. February, 1954.
9. Elliot, J. O. and others. Energy spectrum of neutrons from Po-Be. Physical Review. 93: 1340-1349. 1954.





## IX. ACKNOWLEDGMENTS

My thanks to Dr. Glenn Murphy for his original suggestion of this problem, for the guidance and help which he gave during our association at Iowa State College, and for the loan of certain apparatus used in the experimental part of this investigation.

I would also like to express my appreciation to Dr. A. P. Voigt for his loan of certain apparatus and the sources used in this investigation.

My work at Iowa State College was the third and final year of the Aeronautical Engineering Curriculum of the United States Naval Postgraduate School, Monterey, California, therefore, I would like to express my appreciation to the Naval Postgraduate School for making my work at Iowa State College possible.



## X. APPENDIX

## A. Sample Analytical Computations

The average values of the solid angle  $\bar{\Omega}$  subtended by the detector were calculated by using Equations (11), (12), and (13).

The neutron detector used in this investigation has an active volume in the shape of a right cylinder with dimensions of 1.25 inches diameter and 6 inches height. Thus, for this detector the value of  $h_2$  is 6 inches,  $a$  is 0.625 inches and  $d$  which is equal to  $(\pi a)/4$  is 0.491 inches. For this calculation a cylindrical shell with a 3 inch radius and 16 inch height was used. The values assigned to  $h$  were 0, 1, 2, 3, ..... 14, 15, 16 inches. Equation (11) was used with values of  $h$  from 0 through 3 inches and Equation (12) was used with values of  $h$  from 4 through 16 inches. For  $h$  equal 0 inches, substitution into Equation (11) gave  $\Omega_0$  equal 0.392 and, for  $h$  equal 1 inch,  $\Omega_1$  equal 0.539.

The value of  $\Omega$  was then determined for each of the 17 values assigned to  $h$  and these  $\Omega$ 's were then curved using Equation (13). For this particular cylindrical shell and detector,  $\bar{\Omega}$  was found to be 0.367 steradians. This value is plotted on the upper curve of Figure 2 at  $r/A_2$  equal 0.1875.

The factor  $k$  which is plotted in Figure 3 was calculated using the equation

1. 100

2. 100

3. 100

4. 100

5. 100

6. 100

7. 100

8. 100

9. 100

10. 100

11. 100

12. 100

13. 100

14. 100

15. 100

16. 100

17. 100

18. 100

19. 100

20. 100

$$H = \ln \left[ \left( \frac{1 - \sin \beta_b}{\cos \beta_b} \right) \left( \frac{\cos \beta_f}{1 - \sin \beta_f} \right) \right]$$

For  $\beta_b$  equal -30 degrees and  $\beta_f$  equal 70 degrees, substitution gave  $H$  equal 2.285.

The theoretical values of  $R_T$ , the total neutron scattering ratio, are calculated using Equation (1'). For this sample computation a value of 3 inches for  $h_s$  and the cylindrical shell with 6 inches radius, 0.004 inch shell thickness and 1/6 inches height was selected. The value of  $\bar{\Omega}$  for this geometry and the neutron detector used was taken from Figure 2. This value is 0.159 steradians. The backward angle  $\beta_b$  for this geometry is -39.6 degrees and the forward angle  $\beta_f$  is 61.4 degrees, thus the value of  $H$  as given in Figure 3 is 2.12. The mean free path for scattering,  $\lambda_s$ , was assumed to be constant at the thermal value throughout the energy spectrum of neutrons emitted by this source. For the cladding which is 5 per cent of the total thickness of the sheet,  $\lambda_s$  is 11.76 cm. and for the 243T aluminum  $\lambda_s$  is 10.6 cm. Thus,  $\lambda_s$  for the Alclad 243T is 0.05 times 11.76 cm. plus 0.95 times 10.60 cm. which is 10.66 cm. The detector angle  $\beta_d$  for this detector and geometry is 11.75 degrees. Substituting these values into Equation (16) gave  $R_T$  equal 1.034.

Equation (2h) was used to calculate the theoretical values of  $R_{\gamma}$ ,



the total gamma ray scattering ratio. For this sample calculation, a value of 4 inches for  $h_2$  and the cylindrical shell with 6 inch radius, 0.004 inch shell thickness and 16 inches height was selected. The Geiger tube has a cylindrical active volume of 1.5 inches diameter by 2.375 inches length. The value of  $\bar{\Omega}$  for this geometry, as taken from Figure 2, is 0.952 steradians.

Assuming that the amount of impurities present is one-half of the maximum,  $n_g$ , the number of electrons per cubic cm., for the 24ST aluminum alloy was calculated to be  $6.02 \times 10^{23}$  and for the cladding,  $7.93 \times 10^{23}$ . Thus, the weighted value of  $n_e$  is 0.05 times  $7.93 \times 10^{23}$  plus 0.95 times  $6.02 \times 10^{23}$  which is  $6.02 \times 10^{23}$ .

The backward angle for this geometry is  $-5.0$  degrees and the forward angle is  $46.75$  degrees, thus the value of  $H$  as given in Figure 3 is 2.17. The detector angle for this geometry is  $10.6$  degrees.

The differential cross section  $d\sigma/d\Omega$  for gamma ray scattering is a function of both the gamma ray energy and the angle of scattering. However, it was previously assumed that a constant value could be used for angles of scattering greater than about  $70$  degrees. Plesset and Cohen (5) presented a plot of  $d\sigma/d\Omega$  for various gamma ray energies and angles of scattering. For  $1.02$  mev gamma rays, the average value of  $d\sigma/d\Omega$  for scattering angles greater than  $70$  degrees is  $0.9 \times 10^{-26}$  per electron per square cm. and for  $1.13$  mev gamma rays it is  $0.64 \times 10^{-26}$  per electron per square cm.

Any disintegration of a  $^{60}\text{Co}$  nucleus results in the emission of a cascade of two gamma rays, the first with an energy of  $1.17$  mev and





the second with an energy of 1.33 Mev. By using straight line interpolation between the two values of  $d\sigma/d\Omega$  given above,  $d\sigma/d\Omega$  for the 1.17 Mev gamma rays was found to be  $0.42 \times 10^{-26}$  per electron per square cm. and for the 1.33 Mev gamma rays it was evaluated as  $0.71 \times 10^{-26}$  per electron per square cm. Since the number of gamma rays issued by the source are equal for each of the two energies, the final value of  $d\sigma/d\Omega$  was found by multiplying each of the two values of  $d\sigma/d\Omega$  by 0.5 and adding. Thus  $d\sigma/d\Omega$  used in the equation for  $R_{\gamma}$  is  $0.71 \times 10^{-26}$  per electron per square cm.

Substituting the quantities evaluated above gave a value of 1.0067 for  $R_{\gamma}$ .





the N4

Similitude considerations in neutron and



3 2768 001 89957 8

DUDLEY KNOX LIBRARY